

Ensemble Modelling Framework for Groundwater Level Prediction in Urban Areas of India

¹Basant Yadav, ²Pankaj Kumar Gupta, ³Nitesh Patidar and ⁴Sushil Kumar Himanshu

¹Postdoctoral Fellow in Rural Water Supply, Cranfield University
Cranfield Water Science Institute, Cranfield University, Vincent Building
Cranfield, Bedford, MK43 0AL

*Email ID: Basant.Yadav@cranfield.ac.uk

²Post-Doctoral Fellow, Faculty of Environment, University of Waterloo, Canada
Postal Address: 200 University Ave W, Waterloo, ON N2L 3G1

Email ID: pk3gupta@uwaterloo.ca

³Scientist 'B', Groundwater Hydrology Division
National Institute of Hydrology, Roorkee – 247667
Uttarakhand, India.

Email ID: niteshpatidar88@gmail.com

⁴Postdoctoral Fellow, Texas A&M Agrilife Research,
Texas A&M University System, Vernon, Texas, United States

Email ID: sushil.himanshu@ag.tamu.edu

Abstract: India is facing the worst water crisis in its history, and major Indian cities which accommodates about 50% of its population will be among highly groundwater stressed cities by 2020. In past few decades, the urban groundwater resources declined significantly due to over exploitation, urbanization, population growth and climate change. To understand the role of these variables on groundwater level fluctuation, we developed a machine learning based modelling approach considering singular spectrum analysis (SSA), mutual information (MI), genetic algorithm (GA), artificial neural network (ANN), and support vector machine (SVM). The developed approach was used to predict the groundwater levels in Bengaluru, a densely populated city with declining groundwater water resources. The input data consist of groundwater levels, rainfall, temperature, NOI, SOI, NIÑO3 and monthly population growth rate, and were pre-processed using mutual information, genetic algorithm and lag analysis. Later, the optimized input sets were used in ANN and SVM to predict monthly groundwater level fluctuations. The results suggest that the machine learning based approach with data pre-

processing predict groundwater levels accurately ($R>85\%$). It is also evident from the results that the pre-processing techniques enhances the prediction accuracy and results were improved for 66% of the monitored wells. Analysis of various input parameters suggest inclusion of population growth rate is positively correlated with decrease in groundwater levels. The developed approach in this study for urban groundwater prediction can be useful particularly in cities where lack of pipeline/sewage/drainage lines leakage data hinders physical based modelling.

Keywords: Machine Learning, mutual information, genetic algorithm, artificial neural network, support vector machine, urbanization.

1. Introduction

Groundwater is an important fresh water resource for drinking, agricultural, and industrial purposes in many countries (Boulton and Hancock, 2006; Kulkarni et al., 2015; Mukherjee, 2018). Variation in groundwater levels are subjected differences between the supply and release of groundwater, gaining/loosing stream flow variations, tidal effects, urbanization, earthquake, land subsidence and meteorological phenomena as well as global climatic changes (Todd and Mays, 2005; Taylor et al., 2013; Fendorf and Benner, 2016; Levanon et al., 2017; Tang et al., 2017; Suryanarayana and Mahmood, 2019). A study conducted by Loáiciga (2003) concluded that the rise in groundwater use associated with predicted population growth would pose a higher threat to the aquifer than climate change. The groundwater level response to the hydro(geo)logical (such as groundwater recharge and discharge), meteorological (such as precipitation and temperature) and anthropogenic (such as urbanization and climate change) factors is highly nonlinear and complex (Khatri and Tyagi, 2015; Sapriza-Azuri et al., 2015; Zeng et al., 2017; Liu et al., 2018; Minnig et al., 2018). However, enhanced understanding of complex groundwater level response mechanism considering socio-hydrological heterogeneity is critical for sustainable planning and management of urban water supply (Barthel et al., 2016;

Rathnayaka 2016; Shekhar et al., 2013; Sekhar et al., 2018). In urban areas, water resources management is of utmost importance as its dependency on groundwater for domestic and industrial water supply is increasing due to rapid population growth, increasing per capita water use and limited surface water from distant sources (Eckstein and Eckstein, 2003; Foster et al., 2011).

The advanced numerical methods are capable in modelling complex groundwater flow processes within a given domain. Groundwater level fluctuation has been modelled using physical-based numerical models in several studies (Kim et al., 2008; Wang et al., 2008; Borsi et al., 2013; Yousefi et al., 2019), however, large number of parameter to represent all the physical processes makes groundwater simulations with physical based modelling complex. Moreover, a reliable prediction of groundwater fluctuations requires physical properties of the domain and model parameters to calibrate the model simulations.). Also, uncertainty associated with hydrological, geological, topographical, meteorological and climatic data makes numerical model calibration and validation challenging (Yoon et al., 2011; Barzegar et al., 2017). Further, limitation of data availability, associated cost and time results in model uncertainty and poor model performance (Kumar, 2015; Woodward et al., 2016; Valocchi et al., 2017. Also, assumptions involved in solving the governing equations using the physical based modelling makes the approach less competent in prediction as most of the variables (e.g. groundwater level, evapotranspiration, rainfall) are less predictable. As a result, numerical models tend to produce imperfect results in spite of the capturing the physical processes successfully (Sun et al., 2016). Contrary to that, nonlinear based interdependencies feature of machine learning based models overcomes the requirement of explicit characterization of the physical properties, or accurate representation of physical parameters (Sahoo et al., 2017; Yadav et. al., 2017) and need not to model the underlying physical processes. Over the last decades, machine learning based models have been used in diverse research areas due to their

advantages over numerical models and have been proved efficient in capturing the complex physical processes especially in the data scarce regions (Yoon et al., 2011). However, both physical and data based modelling are based upon different philosophies complement each other with respect to their inherent strengths and limitations (Pandey et al., 2016).. While the important hydrological processes involved in a physically based model make up the black-box feature of a machine learning based model, the difficulty in accurate physical modelling can be alleviated by the powerful machine learning based models (Panda et al., 2010; Napolitano et al., 2010).

A review of literature reports a wide application of machine learning models in modelling nonlinear processes that are complex in nature (Chau et al. 2005; Sivapragasam et al. 2008). Artificial neural network (ANN) has been widely used in past decade for problems related to groundwater level predictions (Coppola et al., 2003; Coulibaly et al., 2001; Daliakopoulos et al., 2005; Nayak et al., 2006; Mohanty et al., 2010; Mohanty et al., 2015). Yoon et al., (2011) and Gong et al., (2016) used ANN in comparative studies while predicting the groundwater level fluctuations. ANN has been adopted by many researchers in the past to predict groundwater levels, however, its high sensitivity to the trained data, overfitting and dependency on hidden neurons are some major drawbacks (Hsu et al. 2002; Wu and Chau, 2011). Similarly, support vector machine (SVM) a relatively newer technique has also been used for the groundwater level prediction in various site conditions (Yoon et al., 2011; He et al., 2014; Gong et al., 2016; Zhou et al., 2017). More recently, fuzzy theory and genetic programming (GP) have also been used to study the groundwater levels (Kurtulus and Razack, 2010; Güler et al., 2012; Shiri and Kisi, 2011; Fallah-Mehdipour et al., 2013; Kasiviswanathan et al., 2016). Further, latest techniques like extreme learning machine (ELM) which are much simple in design and application then ANN or SVM have also been used in groundwater modelling studies (Yadav and Eliza, 2017; Alizamir et al., 2018). Further, Suryanarayana et

al., (2014) developed a wavelet (WA) based integrated WA-SVM model to predict monthly groundwater levels and their results suggest that WA-SVM performs better than auto regressive integrated moving average (ARIMA), ANN and SVM. Similarly, a study conducted by Sahoo et al., (2017) used a data pre-processing approach in developing a hybrid artificial neural network model (HANN) to predict seasonal groundwater level change in agricultural region of high plains and the Mississippi river valley alluvial aquifer.

Accuracy of machine learning based groundwater level simulation or prediction, predominately depends on the type of input data used. It was pointed out in many studies that the generalization ability of machine learning based models are significantly influenced by selection of appropriate input variable (Maier and Dandy, 2000; Galelli et al., 2014; Quilty et al., 2016; Sahoo et al., 2017). The most obvious input variables in groundwater level predictions studies are rainfall, evaporation, temperature and pumping patterns (Yoon et al., 2011; Singh et al., 2014; Mohanty et al., 2015; Kasiviswanathan, 2016; Chang et al., 2016; Barzegar et al., 2017; Wunsch, 2018). Further, groundwater levels are also partially controlled by interannual to multidecadal climate variability (Kuss and Gurdak, 2014; Sahoo et al., 2017; Velasco et al., 2017). Therefore, appropriate input variable along with the application of pre-processing techniques has resulted in improved groundwater level prediction accuracy by capturing the seasonal variability and reducing the impact of noisy data (Wu et al., 2009; Wang et al., 2014; Sahoo et al., 2017). Overall, these studies have demonstrated the ability of data based modelling for developing a generalized non-linear relationship among hydro(geo)logical, meteorological and climatic input variables and groundwater.

In most studies, application of simple to complex groundwater models have been demonstrated in large agricultural catchments and there are very few studies predicting groundwater levels in urban areas (Coulibaly et al., 2001; Daliakopoulos et al., 2005; Wang et al., 2014; Shao et al., 2017; Wunsch et al., 2018; Yousefi et al., 2019). A study by Lerner (2002) describes how

urbanization affects groundwater cycle by way of changes to both the total water budget, and to pathways recharge. Groundwater management in such circumstances is crucial to control the decline groundwater levels and therefore, this requires a scientific understanding of urban groundwater systems based on a hydrological, meteorological, climatological and anthropogenic factors. In this study, we studied the impact of population growth, climatic variability and hydro-meteorological variables on the groundwater level fluctuations by combining the pre-processing techniques and advanced machine learning models. To study the groundwater level fluctuation of a complex urban catchment, we have selected variables like population growth rate (P), rainfall (R), temperature (T) and climatic variables. To the best knowledge of the authors, this study is the first to couple SSA and SVM considering variables like population growth rate to study an urban catchment. The novelty of the research work is to study a highly urbanized catchment with limited groundwater resources using hydro-meteorological, climatic and population data in hybrid SSA-MI-GA-ANN and SSA-MI-GA-SVM models to predict the monthly groundwater level fluctuations. Henceforth in this article 'H' (SSA-MI-GA) will be used as a prefix in front of ANN and SVM to represent hybrid models. The objectives of this research was to study the performance of original (ANN, SVM) and hybrid (HANN, HSVM) models to predict groundwater levels of Bengaluru urban district for one and two months ahead.

2. Material and Methods

2.1 Study Area

The study area (Fig. 1) is located in the south-eastern part of Karnataka and have geographical extent of 2174 km². Total population of the area is 9.622 million (2011) with population density of 4,378 people per km². The average annual rainfall of the area is 970 mm getting contribution from the South-Western monsoon (54.18%), the North-Eastern monsoon (26.53%) the pre-monsoon showers (18.53%) (Bengaluru water supply and sewerage board, Report, 2017). The average maximum and minimum temperature is about 38°C during summer and 15 °C during

winter, respectively. The relative humidity is about 86% during monsoon and 63% during dry months.

Physiography of the area comprises of rocky upland, plateau and flat topped hills (approx. 900m above mean sea level). Soils of the area could be categorised into red loamy soil and lateritic soil. This type of soil can be found in the eastern and southern part of study area which have hilly to undulating topography with granite and gneissic terrain. Further, lateritic soils are observed in western part of the study area where the terrain is undulating and gently sloping topography of peninsular gneissic region (Bengaluru water supply and sewerage board, Report, 2017). Groundwater occurs in phreatic conditions in weathered zones and under semi-confined to confined conditions in fractured and jointed rock formations.

Granites and Gneisses of peninsular gneissic group form the primary aquifers in the study area. Alluvium of thickness 20–25 m thick occur along the river courses possessing substantial groundwater potential. About 90% of groundwater structures tapping as shallow aquifers are yielding less than 1 litter per second. While, deep aquifers of yield ranged from 2 to 8 litter per second are located in parts of Bengaluru north and Anekal taluks. Transmissivity ranged from 10 to 280 m² /day (CGWB, 2008; Gulgundi and Shetty, 2018).

The study area contains Archean crystalline formation (Dharwar Province of the southern Indian peninsula) comprising peninsular gneiss's complex with small patch of hornblende schist in the northern part and intrusive closepet granites all along the western part (Chadwick et al. 1997; Mukherjee et al. 2018). The eastern edge of the Bengaluru city dominates to laterite of tertiary age, which occur as isolated patches capping crystalline rocks. Some small stretch of about 25km comprising unconsolidated sediments (Channapatna and Devanahalli) are found in study area.

Groundwater levels vary seasonally and found deepest during summer (April-May) and shallow during post monsoon (October-November). In general, decline in groundwater level

across the study area starts from late November and this falling trend in during post monsoon can be attributed to erratic monsoon and rapid urbanization and land use change thus minimizing groundwater recharge (Bengaluru water supply and sewerage board, Report, 2017).

The modelling approach using ANN, SVM, HANN and HSVM were assessed in Bengaluru urban district to predict monthly groundwater levels changes. Monthly groundwater level data of 2010 to 2017 (8 years) for 24 wells were acquired from the District Groundwater Office, Groundwater Directorate Bengaluru, Karnataka. The selected wells are uniformly distributed in the study area and represents the groundwater conditions across the district. Monthly gridded rainfall data with a resolution of $0.25^{\circ} \times 0.25^{\circ}$ (Pai et al., 2014, 2015) and average temperature time series with a resolution of $1^{\circ} \times 1^{\circ}$ (Srivastava et al., 2009) was also collected for the period of 2010 to 2017. Further, the climatic parameters such as Southern Oscillation Index (SOI), Northern Oscillation Index (NOI), and Niño3 were collected also collected for each month for years 2010 to 2017 from National Oceanic and Atmospheric Administration (NOAA, 2018a, 2018b and 2018c). SOI and NOI relate variability in the atmospheric forcing of climate change in northern and southern mid-latitude hemisphere regions and show interesting relationships in equatorial and extratropical teleconnections and represent a wide range of local and remote climate signals (Schwing et al., 2002). Niño3 is an index which is used to define El Niño and La Niña events covering large spatial area and with different seasonal evolution. Apart from the climatic and hydro-meteorological data, we also considered population growth rate to consider the impact of urbanization on groundwater levels. The annual population growth rate data was obtained from World Population Review (2018) and later was converted into monthly growth rate.

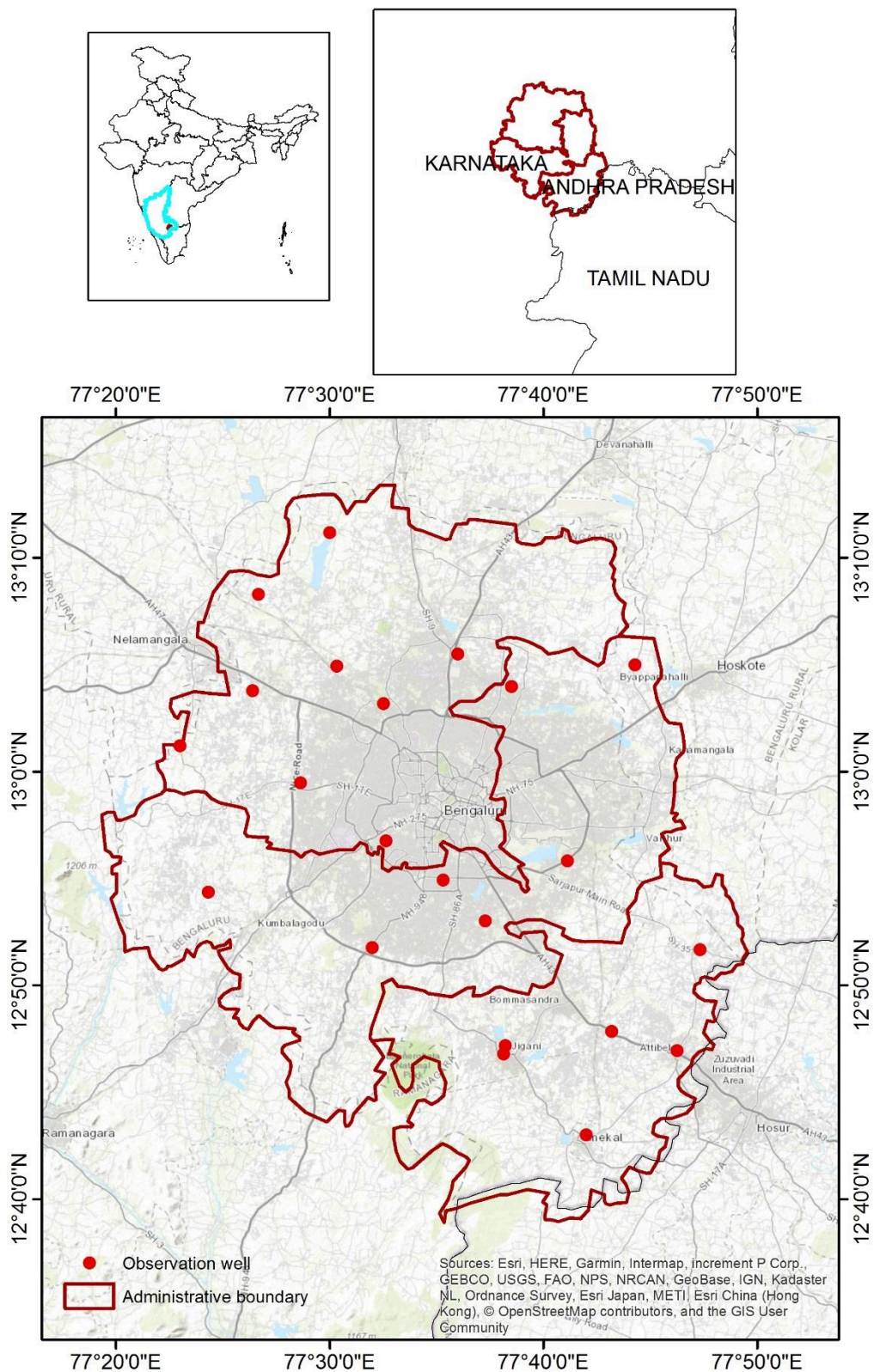


Fig. 1 Study area map of Bengaluru urban district with the monitoring well locations

2.2 Data processing and parametric optimization

The input data for the groundwater level prediction consist of groundwater levels, rainfall, temperature, NOI, SOI, NIÑO3 and monthly population growth rate. Data for the rainfall and temperature were processed and converted into time series. The input variables were pre-processed using singular spectrum analysis (SSA). Singular spectrum analysis decomposes the time series into a sum of a small number of interpretable components such as a slowly varying trend, oscillatory components and noise (Marques et al., 2006; Wang et al., 2015). SSA is a non-parametric technique of time series analysis based on principles of multivariate statistics (Vautard & Ghil, 1989; Dettinger et al., 1995). The given time series is decomposed into a set of independent time series to represent either a trend, periodic or quasi-periodic component or noise. As pointed out by Hanson et al., (2004) and applied by Sahoo et al. (2017) the variability of a hydrologic time series can be captured in first 10 reconstructed components (RCs) which are associated with the trend, oscillations or noise of the original time series. In this study, first 10 RCs of each input variable were extracted and later further processed using MI-GA approach to identify the most relevant RCs with respect to the groundwater levels.

The decomposed time series were further processed using mutual information and genetic algorithm to minimize the redundancy in the input data. Mutual information measure linear and non-linear dependencies between input and output variable. In this study, MI was used to establish nonlinear dependence between reconstructed components of the input variable and groundwater water levels. The interdependence between input and output variable using information theory obtained by measuring marginal entropy, conditional entropy and joint entropy. It takes a minimum value zero when there is no dependence between two variables, while a positive value suggest strong dependence among the considered input and output variables.

238 The entropy of a discrete random variable $x = (x_1, x_1 \dots x_N)$ is denoted by $H(X)$. Where x_i refers
 239 to the possible values that X can take. $H(X)$ is defined as (Vergara and Estévez, 2014):

$$240 \quad H(X) = - \sum_{i=1}^N p(x_i) \log_2(p(x_i)) \quad (1)$$

241 where $p(x_i)$ is the probability mass function. For any two discrete random variable X and
 242 $Y = (y_1, y_1 \dots y_M)$, the joint entropy is defined as (Vergara and Estévez, 2014):

$$243 \quad H(X, Y) = - \sum_{j=1}^M \sum_{i=1}^N p(x_i, y_j) \log_2(p(x_i, y_j)) \quad (2)$$

244 where $p(x_i, y_j)$ is the joint probability mass function of the variables X and Y . The
 245 conditional entropy of the variable X given Y is defined as (Vergara and Estévez, 2014):

$$246 \quad H(Y | X) = - \sum_{j=1}^M \sum_{i=1}^N p(x_i, y_j) \log_2(p(y_j | x_i)) \quad (3)$$

247 The joint entropy has values in the range,
 248

$$249 \quad \max(H(X), H(Y)) \leq H(\{X, Y\}) \leq H(X) + H(Y)$$

250 $H(Y|X)$ is the amount of uncertainty left in Y when X is introduced, so it is less than or equal
 251 to the entropy of both variables, however it can be equal to the entropy if, the two variables
 252 have absolutely no dependencies.

253 Mutual information measures the level of interdependencies between two random
 254 variables. In case of feature selection, the approach is useful as it gives a quantifiable estimate
 255 of relevancy for a feature with respect to the output. Mutual information between two random
 256 variables is defined as (Vergara and Estévez, 2014):

$$257 \quad I(X; Y) = \sum_{j=1}^M \sum_{i=1}^N p(x_i, y_j) \cdot \log \left(\frac{p(x_i, y_j)}{p(x_i) \cdot p(y_j)} \right) \quad (4)$$

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where $I(X;Y)$ is mutual information between input X and output Y . For more information on information theory reader can refer to Vergara and Estévez (2014).

The relevancy of feature is counted if it provides information about output individually or together with other variables. However, the variable is counted redundant if it doesn't provide much information. Following the principle of maximum relevance (Eq. 5) and minimum redundancy (Eq. 6), most relevant RC of every input parameter was obtained using mutual information values and a genetic algorithm (Ludwig et al., 2009).

$$R_{el} = \frac{1}{N} \sum_{i=1}^N I[X_i; Y], \quad (5)$$

$$R_{ed} = \frac{1}{N^2} \sum_{i=1}^N \sum_{j=1}^N I[X_i; X_j], \quad (6)$$

$$F_{max} = R_{el} - R_{ed}, \quad (7)$$

where R_{el} represents average mutual information values showing the level of relevance between input (RCs) and output (groundwater levels) variables. R_{ed} represents average of all the mutual information values of the individual inputs. A fitness function F_{max} was solved using genetic algorithm to maximize the relevance and minimize the redundancy of the inputs.

In genetic algorithm variables are represented as chromosomes containing information about various decision variables that represent a decision or a solution. The fitness of randomly generated chromosomes is evaluated individually with respect to a target value. In this study, 40 randomly generated chromosomes were used for generation of 10 RCs. Objective function F_{max} was used to calculate the fitness of each chromosomes and later cross-over was performed, which introduces diversity in the population of the programs signifying the internal information exchange between the structures in the new and old population. The best model is identified by repeating the runs for a certain number of generations (80 in this study) or until a good

solution is obtained with fixed values of the controlling parameters. The optimization approach gave two best RCs that maximize the value of fitness function. Lastly, the pre-processed and optimized input variables were used in ANN and SVM to predict the monthly groundwater level.

3. Model Development

3.1 Artificial Neural Networks (ANN)

Artificial Neural Networks is a machine learning approach established as a robust tool for many hydrologic processes as simulation and prediction tool particularly when the underlying processes have complex nonlinear interrelationships (Govindaraju, 2000; Hsu et al., 2002). A common network of ANN comprises interconnected nodes called neurons arranged into input layer, hidden layer and output layer. The information is entered into data entry layer (input layer) which forwarded into hidden layer for the data processing and thereafter into output layer which generate the results for the given input (Dawson and Wilby, 1998). This type of network is called feed forward back propagation (FFBP) network in which the information passes only in forward direction from input layer, through hidden layer and finally to the output layer. The input vectors are $D \in R^n$ where $D = (X_1, X_2, \dots, X_n)^T$, the outputs of N neurons in the hidden layer are $Z = (Z_1, Z_2, \dots, Z_n)^T$ and the output from output layer are $Y \in R^m$ where $Y = (Y_1, Y_2, \dots, Y_n)^T$. The weight and the threshold between the input layer and the hidden layers are w_{ij} and y_j , respectively. The following equations represent the neuron outputs in the hidden and output layer (Schalkoff, 1997):

$$Z_j = f \left(\sum_{i=1}^n w_{ij} X_i \right) \quad (8)$$

$$Y_k = f \left(\sum_{j=1}^N w_{kj} Z_j \right) \quad (9)$$

where a transfer function f is used to offer the rule for mapping the neuron's total input to its output.

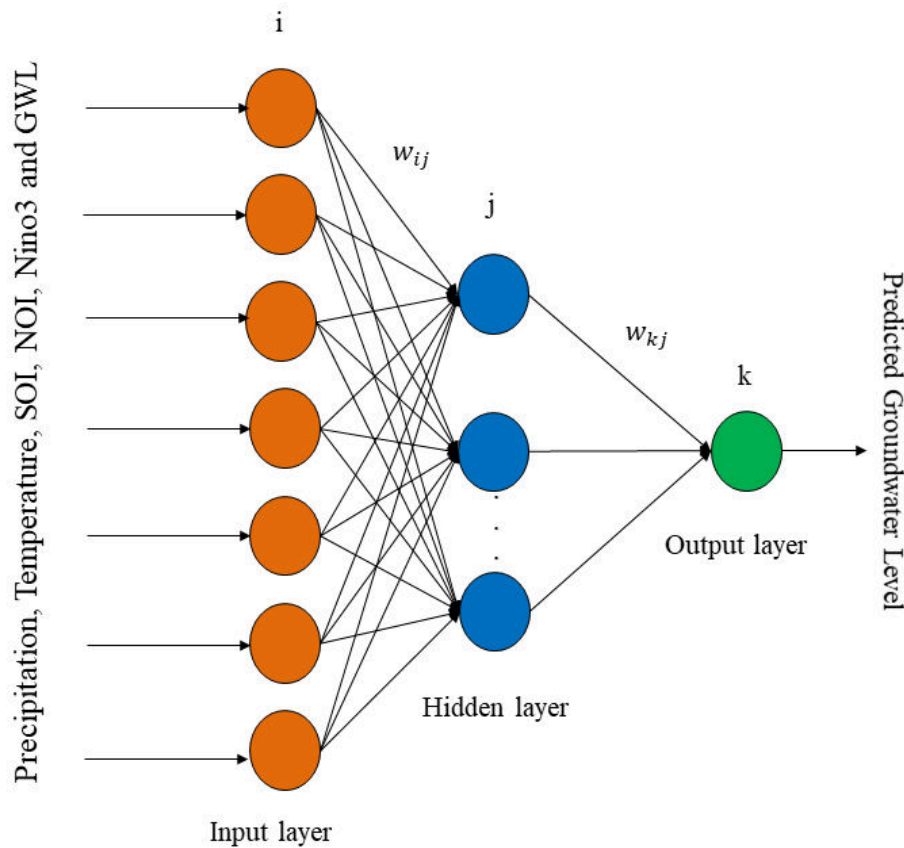


Fig. 2 A typical three-layer feed-forward ANN.

In this study, a three layer (input layer, hidden layer and output layer) ANN model (Fig 2) is developed to predic the groundwater level flectuations in Bengaluru urban district. The input and output data variables were divided into three groups training (70%), validation (15%) and testing(15%). The input layer consist of 7 neurons each for both models (ANN, HANN) and 1 output neuron (groundwater level). The developed model utilizes “newff” function to assign the initial weights randomly. An hyperbolic tangent sigmoid transfer function was used to process informtaion between input and hidden layer. Later, a linear transfer funtion “purelin” was used to transform the procssed infoirmation from hidden layer to the output layer (Schmid, 2009). The key parameters such as the learning rate and momentum in the network are obtained

by a trial and error procedure for each locations (wells). The model performance was assessed using correlation coefficient (R), Root mean squared error (RMSE) and Normalised Mean Square Error (NMSE).

3.2 Support Vector Machine (SVM)

Support vector machine (SVM) is a machine learning approach proposed by Vapnik (1995) and as classification and regression procedure. SVM which based on the structural risk minimization principle has good generalization ability and is less prone to overfitting, (Vapnik and Vapnik, 1998; Vapnik, 2000; Yao et al., 2008). In regression problems, SVM uses kernel function to map the input vector in to a high dimensional feature space where the input vector is linearly separable (Wu et al., 2014). The developed SVM in this study was used to find a regression function that estimate the functional dependence between input and output variables $\{(x_1, t_1), \dots, (x_n, t_n)\}$. Where $x_i \in R^n$ in this study represents input variable (rainfall, temperature, past groundwater level, SOI, NOI and Niño3, population growth rate) while and $t_i \in R^n$ referred to as space of target output (groundwater level) value of n data lengths. SVM calculates the linear regression by solving (Vapnik, 1995) the following equations:

$$f(x) = w\varphi(x) + b \quad (10)$$

$$R_{SVM_s}(C) = \frac{1}{2}\|w\|^2 + C \frac{1}{n} \sum_{i=1}^n L(x_i, t_i) \quad (11)$$

where $\varphi(x)$ is non-linear mapping function of x ; w is weight vector and b is a bias term;

$C \frac{1}{n} \sum_{i=1}^n L(x_i, t_i)$ is the error component. To estimate the weight vector and bias, two positive

slack variables ξ and ξ^* are added to limit the estimation error by the $\mathcal{E}$ -insensitivity loss function (Vapnik and Vapnik, 1998) thus:

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$$\min \frac{1}{2} \|w\|^2 + C \sum_{i=1}^n (\xi + \xi^*) \quad (12)$$

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$$\text{Subject to } \begin{cases} t_i - w\varphi(x_i) + b_i \leq \varepsilon_i + \xi_i \\ w\varphi(x_i) + b_i - t_i \leq \varepsilon_i + \xi_i^* \\ \xi_i, \xi_i^* \geq 0, i = 1, \dots, l \end{cases}$$

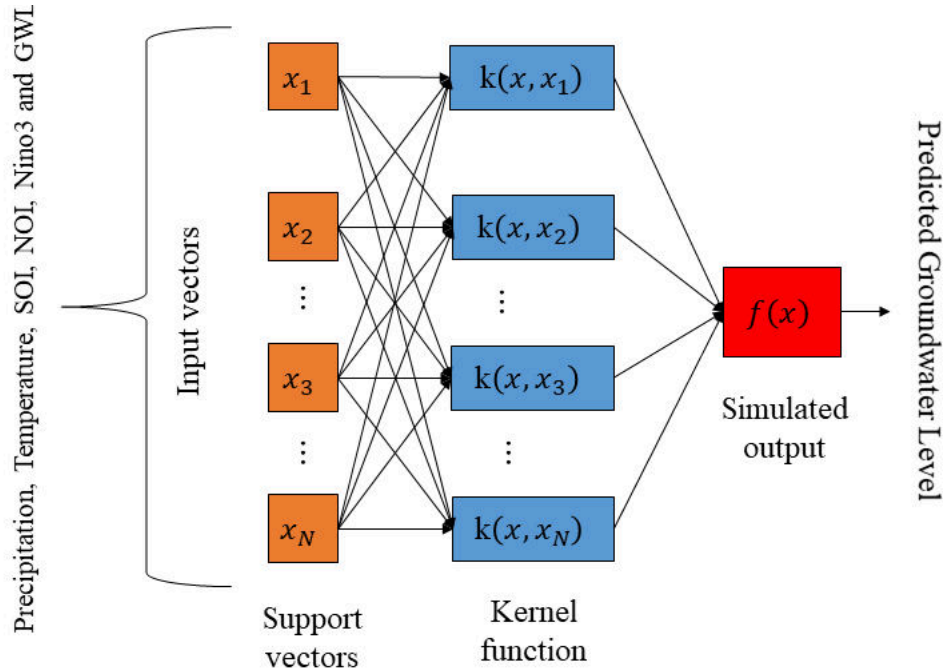
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where C is the positive trade-off parameter for the degree of empirical error and l is the

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factor number in the training data.

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Fig. 3 The schematic representation of SVM

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In previous hydrological prediction studies, radial basis functions (RBF) has been

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recommended as the most suited kernel function due to its capability to process highly complex

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parameter space (Rajasekaran et al., 2008; Yang et al., 2009; Wang et al., 2009; Yadav et al.,

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2016, Yadav and Eliza, 2017; Himanshu et al., 2017a; Yadav and Mathur, 2018). RBF is

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defined as:

$$K(x_i, x_j) = \exp\left(-\gamma \|x_i - x_j\|^2\right) \quad (13)$$

where x_i and x_j are vectors in the input space, such as the vectors of features computed from training and testing. γ is defined by, $\gamma = \frac{1}{2\sigma^2}$ for which σ is the Gaussian noise level of standard deviation. Figure 3 shows the schematic representation of SVM.

The SVM models for monthly groundwater level prediction using the pre-processed input data obtained from SSA and MI-GA approached was developed using LIBSVM toolbox. The model structure (Eq. 14 and 15) which were used in ANN, HANN model were kept same for SVM and HSVM as well. Prediction accuracy of SVM model depends on the suitable selection of kernels and parameters. It has been suggested in many studies that the radial basis function (RBF) performs well in hydrological forecasting problems and is hence it was considered in this study as well. The parameter of radial basis function was obtained using trial and error method for each well location. The developed models were used predict the monthly groundwater level using raw (SVM) pre-processed (HSVM) input variables for one and two months ahead.

3.3 The Ensemble Model

The ensemble prediction model using SSA, MI-GA, ANN and SVM was developed in MATLAB2014a. A separate code was written for SSA to decompose the input time series. MI-GA model was developed following the approach suggested by Ludwig et al., (2009). Further, ANN and SVM models were developed in MATLAB using 'newff' function and LIBSVM library, respectively. The input variable, monthly population growth rate, SOI, NOI, Niño3 were recorded as monthly time series. Temperature and rainfall data were extracted from the gridded (0.25°×0.25°) IMD data set and converted into monthly time series. The area covered under the gridded data for latitude 12.75° to 13.25° and Longitude 77.25° to 77.75° produced nine-time series for both temperature and rainfall, however, initial analysis revealed little

variability among them, therefore only one-time series for each temperature and rainfall was considered during groundwater level prediction. Lastly, the monthly groundwater level for the past two months was also added in the input data set. Each input variable was first decomposed using SSA and converted in 10 RCs. These RCs were supplied to an integrated MI-GA based model with the objective function to maximize the relevancy and minimize the redundancy resulted into two best RCs with respect to output variable (groundwater level). This procedure was repeated for each input variable and all the well locations. Once the optimized RCs with respect to each well water level was identified, the input-output combination was divided into training (70%), validation (15%) and testing (15%) data set. These combinations were used in both HANN and HSVM to predict the groundwater level at each location for one month and two months ahead. These hybrid models were later compared with the original model ANN and SVM in which raw input data was used for training, validation and testing. Figure. 4 depicts the procedure followed:

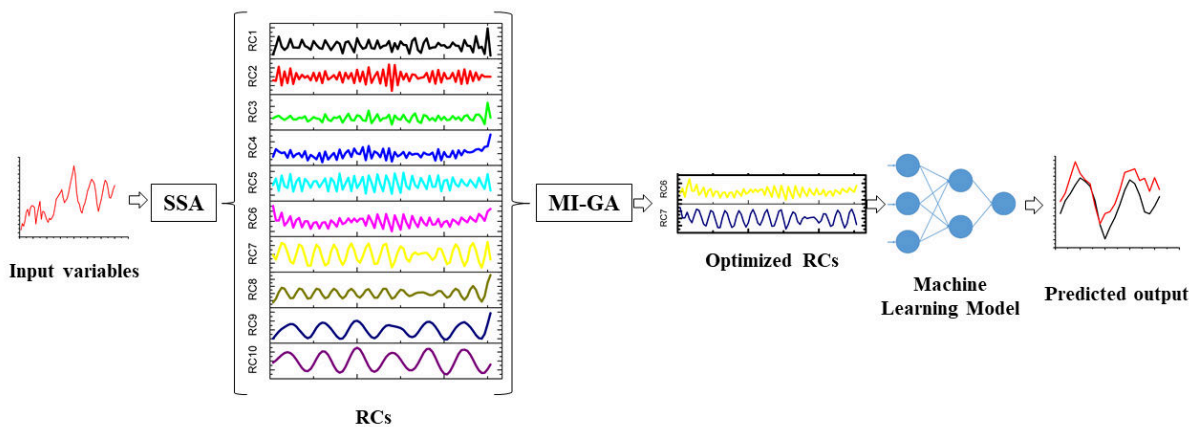


Fig. 4 Ensemble model using SSA, MI-GA and Machine learning models (ANN, SVM) to predict the groundwater levels.

4. Result and Discussion

4.1 Input selection and model development

In this study, a machine learning based approach considering data pre-processing techniques were developed to predict the groundwater level fluctuations in an urban area. The input data

consist of rainfall (R), temperature (T), SOI, NOI, Niño3, population growth rate (P) and groundwater level (GWL). Temporal lag correlational analysis was performed among the best RC of groundwater and the best RC of population growth rate, southern oscillation index, Northern oscillation index, Niño3, rainfall, temperature and past groundwater level, respectively. Population growth rate was found to be strongly correlated with groundwater levels at zero lag, which suggest that the increasing population and hence increased groundwater abstraction had immediate impact on the groundwater level. Similarly, temperature and Niño3 also showed strong correlation with groundwater level at zero-time lag, however SOI time lag was found to be three months. Further, resulting time lags for NOI index and R were two months. The obtained prediction model for one month (eq. 14) and two months (eq 15) expressed as follows:

$$GWL_{t+1} = f(P_t, NOI_{t+2}, SOI_{t+3}, Nino3_t, T_t, R_{t+2}, GWL_t) \quad (14)$$

$$GWL_{t+2} = f(P_t, NOI_{t+2}, SOI_{t+3}, Nino3_t, T_t, R_{t+2}, GWL_{t+1}) \quad (15)$$

Later, all input variables were processed using SSA which generated 10 RCs of each input variable. Subsequently, the obtained RCs were optimized using MI-GA approach corresponding to each well locations. The optimized RCs of all the input variables were then used in ANN and SVM model to predict the groundwater level for one and two months ahead. ANN model was developed for each well location and hidden neurons were optimized using a trial and error method. Hidden neurons play very significant role in the model prediction accuracy and large number of input variable with high variability requires more hidden neurons. The minimum hidden number 7 were obtained for Chikkabanavara well location, however the highest number 21 was obtained at Thimmenahalli. Wells with the groundwater level standard deviation more than 7 (Fig. 5) required 15 to 21 neurons. However, if the

groundwater level standard deviation varied between 1 to 5, resulting optimum neurons varied from 5 to 9.

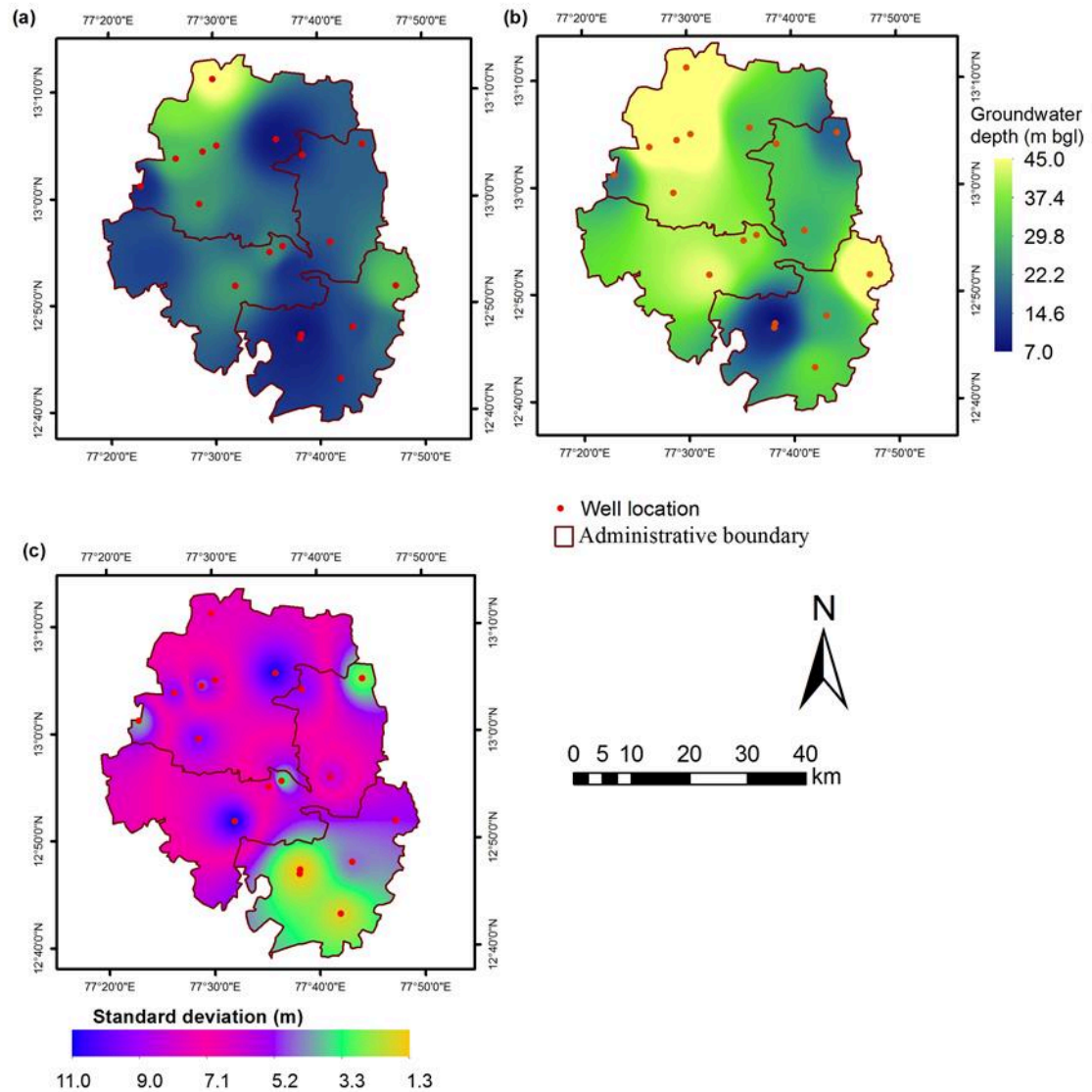


Fig. 5 Groundwater level during 2010 (a) and 2015 (b). Standard deviation in the groundwater level from 2010 to 2015 (c). A common color bar is shown for map (a) and (b) in the right.

Similarly, SVM model parameters namely regularization constant, insensitive loss function and RBF parameter (γ) were also obtained corresponding to each well location. Regularization constant varied between 1.42 to 2.65 for all the location while insensitive loss function values between 0.032 to 0.098. Tuning of regularization constant is crucial for successful model development as it is a trade-off between the model complexity (flatness) and the degree to

which deviations larger than insensitive loss function are tolerated in optimization formulation. Value of C was kept low to achieve a balance output where the empirical error was minimized considering the model complexity. Insensitive loss function values were kept low for all the well locations as larger value can cause fewer selection of support vector which will result in less complex regression estimate. The parameter obtained during the model development (ANN and SVM) were kept similar for the prediction (1 month and 2 month) as well.

4.2 Groundwater level prediction

Long term simulations (2010-2015) were run to predict the 1-month and 2-months ahead groundwater depths for eighteen different locations across Bengaluru city in India. A substantial difference in predicted groundwater levels were observed under different machine learning approaches (Figures 6-9). Results presented here as box plots indicates the significant variability in simulated results across the simulation period under different machine learning approaches. The horizontal line and small solid square inside the box indicate the median and mean, respectively, and the ends of boxes indicate the 25th and 75th percentiles. Small line outside the boxes represent outliers or values greater than 1.5 interquartile ranges away from the 25th or 75th percentiles. In general, the simulated results were significantly improved under hybrid approaches (HANN and HSVM) as compared to conventional ANN and SVM approaches for both 1-month and 2-months ahead predictions. The results of the simulations are consistent with several other studies, which reported that the model predictability was further improved under hybrid approaches as compared to conventional machine learning approaches (Sahoo et al., 2017; Himanshu et al. 2017b; Yadav and Eliza, 2017). The results showed that 1-month ahead predictions were very precise and shows a better agreement with the observed groundwater level data. However, for 2-months ahead predictions, the predicted results were not very close to observed values, especially under conventional ANN and SVM approaches. Among HSVM and HANN, performance of HSVM was found better than HANN

at most of the locations for both 1-month and 2-months ahead predictions, except at Sarjapura, Talaghattapura and Manduru locations for 2-months ahead predictions, where performance of HANN was found better (Figure 8d, 9d, 9g). In general, among all the four approaches, performance of ANN was comparatively not found good for both 1-month and 2-months ahead predictions at all the locations.

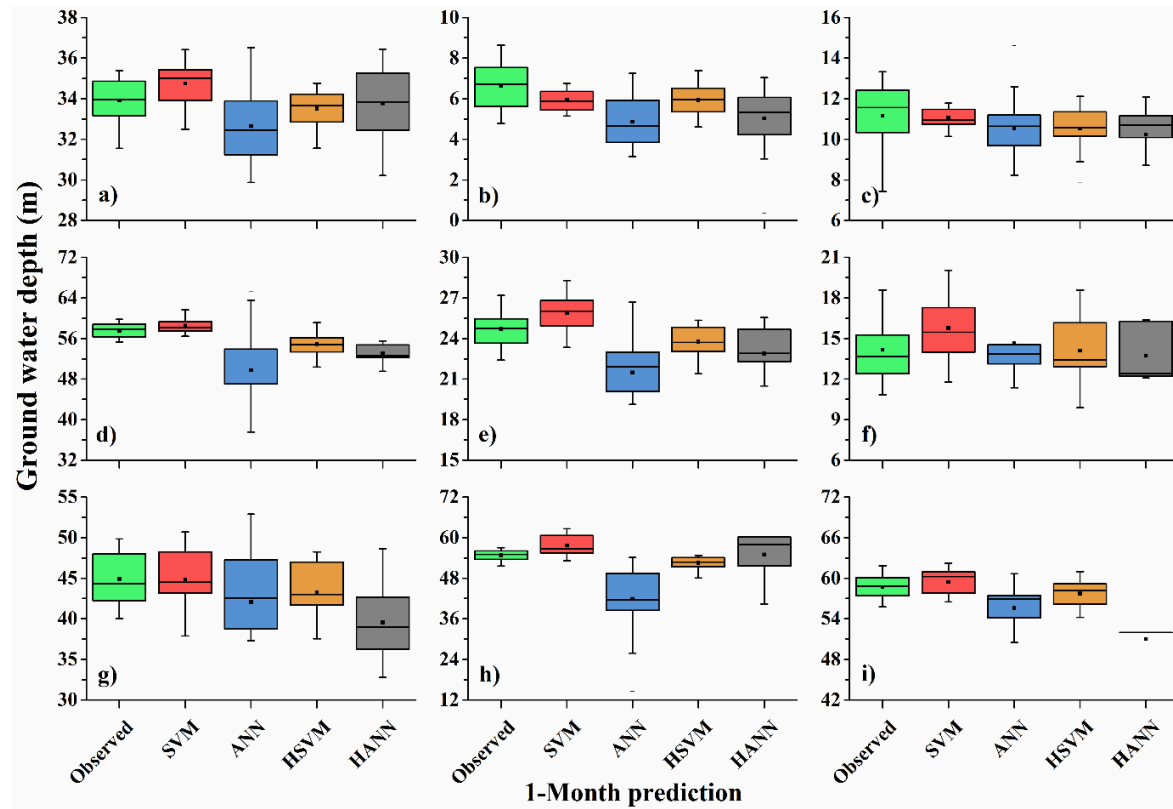


Fig. 6: 1-Month ahead predicted groundwater depths for locations a) Anekal, b) Jigani, c) Bannerughatta, d) Sarjapura, e) Chandapura, f) Thimmenahalli, g) Byadarahalli, h) Chikkabanavara, and i) Rajanukunte

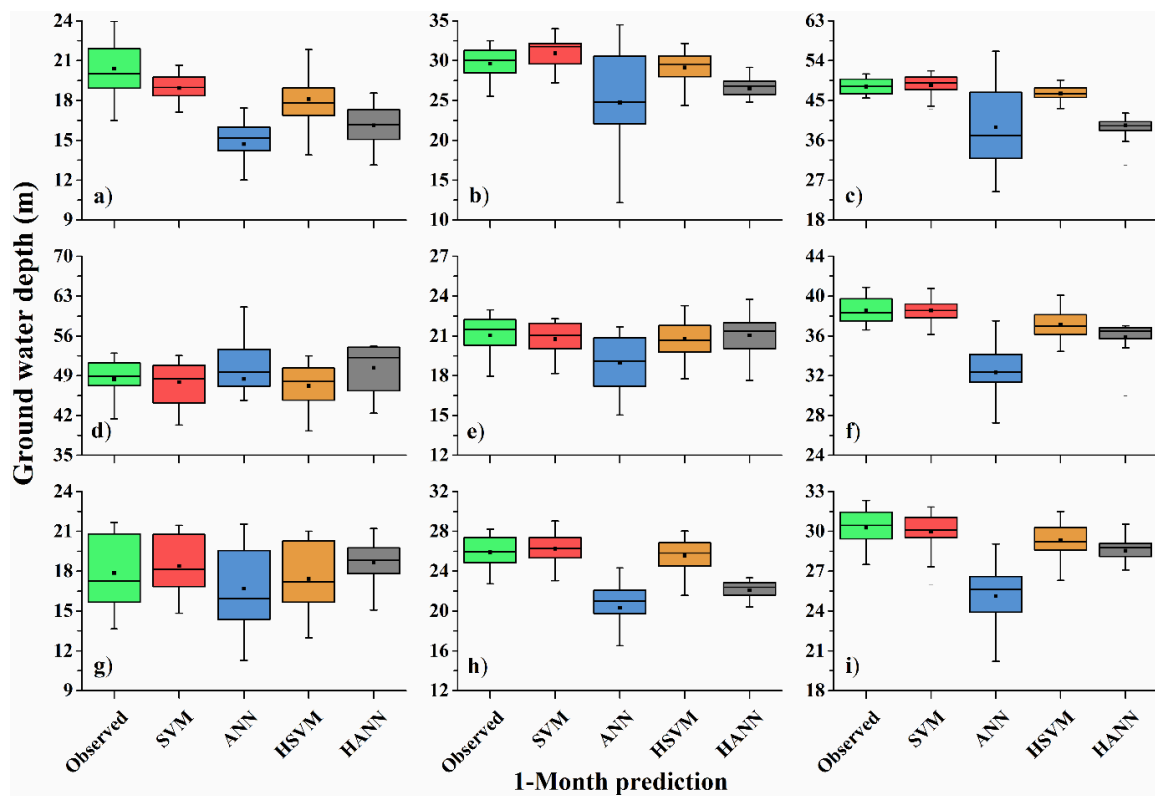


Fig. 7: 1-Month ahead predicted groundwater depths for locations a) Sondekoppa, b) Yelahanka, c) Adikemaranahalli, d) Talaghattapura, e) Tavarekere, f) Marenahalli, g) Manduru, h) Devarabeesanahalli, and i) K.Narayanapura

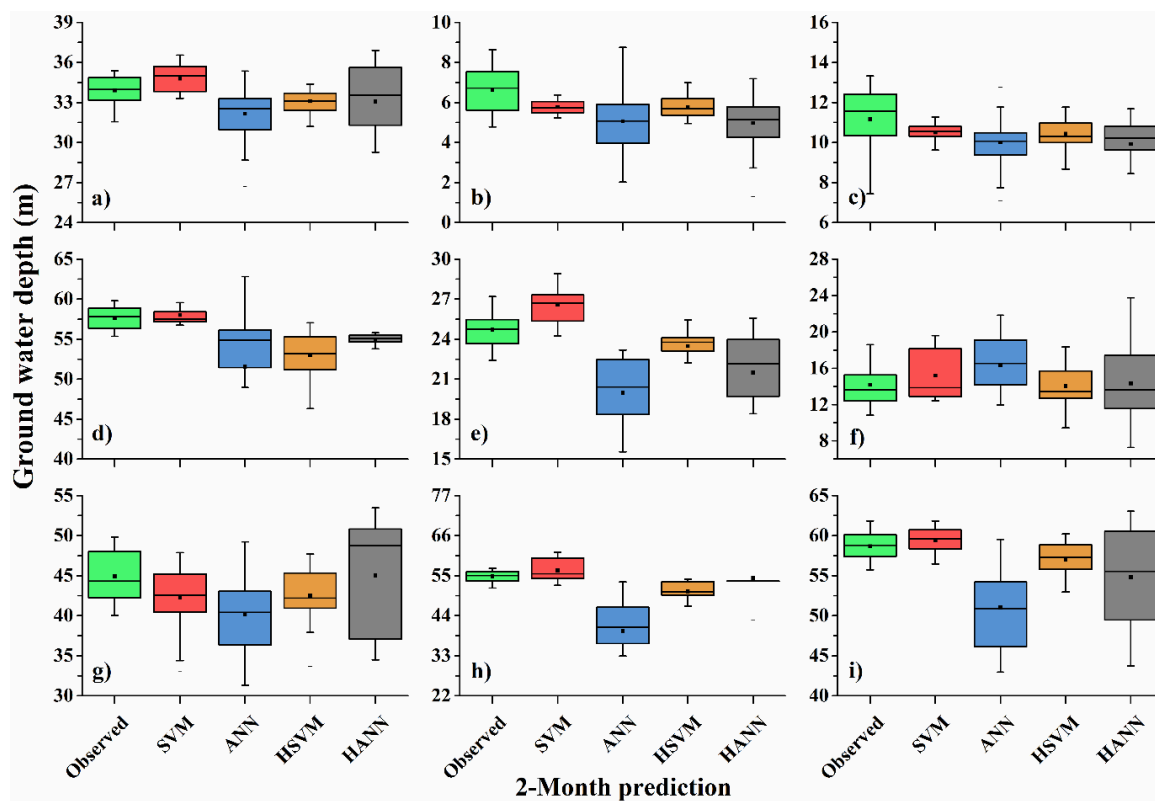


Fig. 8: 2-Month ahead predicted groundwater depths for locations a) Anekal, b) Jigani, c) Bannerughatta, d) Sarjapura, e) Chandapura, f) Thimmenahalli, g) Byadarahalli, h) Chikkabanavara, and i) Rajanukunte

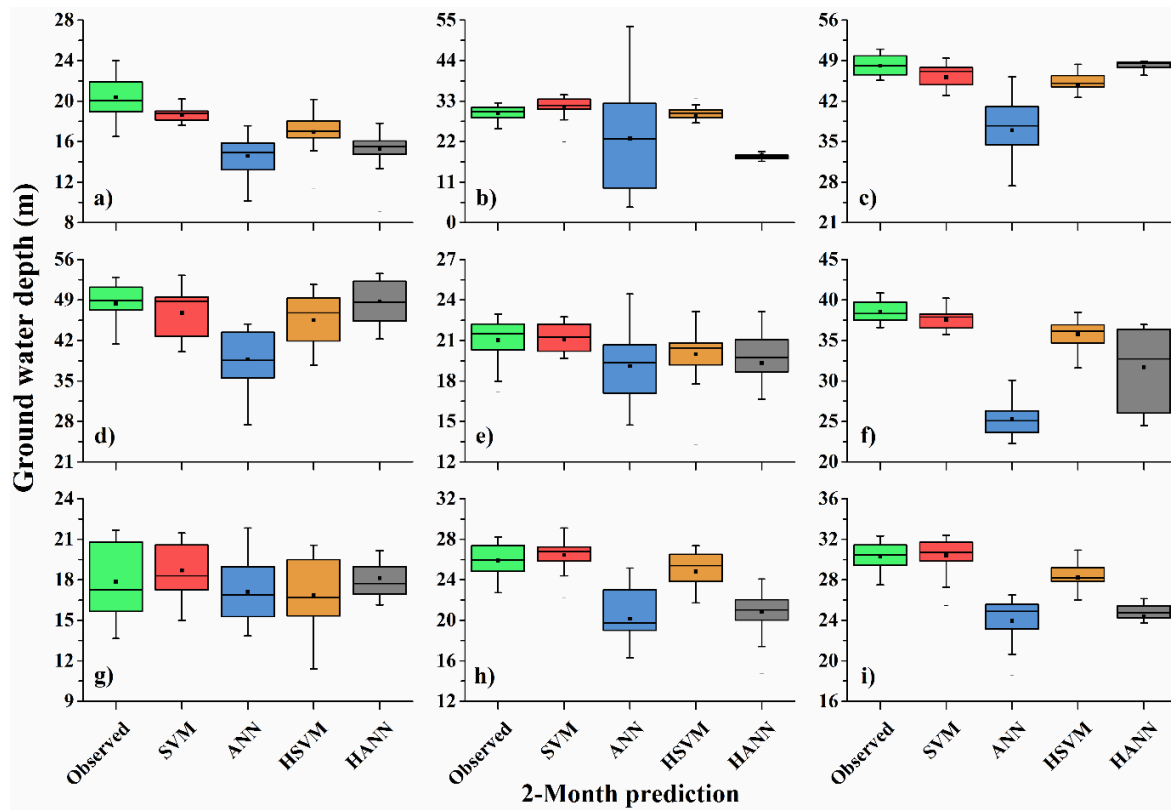


Fig. 9: 2-Month ahead predicted groundwater depths for locations a) Sondekoppa, b) Yelahanka, c) Adikemaranahalli, d) Talaghattapura, e) Tavarekere, f) Marenahalli, g) Manduru, h) Devarabeesanahalli, and i) K.Narayanapura

Table 1 show the average statistics of model performance during 1 and 2 months ahead groundwater level prediction. The results show that the performance of ANN model was improved significantly when used with pre-processed data (HANN). Performance statistics of ANN during 1 month ahead prediction improved approximately by 55%, 35% and 64% for R, RMSE and NMSE, respectively. In case of SVM, the improvement was 1.85%, 0.36% and 17% for same statistical indicators. Similar improvements were observed when the models were used for 2 months ahead prediction, the performance of ANN improved upto 50%, 31% and 56 % for R, RMSE and NMSE, respectively. However, the improvement in case of SVM was 0.97%, 3.77% and 11% for R, RMSE and NMSE, respectively. HSVM is the superior method to predict groundwater fluctuations throughout the study area and fortifies that model could map these complex interdependences of climatic variations, population growths on groundwater level fluctuations. These results indicate that the HSVM and SVM model of this

study is more likely to learn the complex relationship of groundwater fluctuation with urban environment for the given data than the ANN. The evaluation of the proposed technique in an urban area having a complex hydrological regime shows that the technique provides improved results for groundwater level prediction when compared to traditional techniques.

Table 1 Original and hybrid model comparison for one and two month prediction using average statistics for 19 well locations

1 Month ahead prediction				
	ANN	SVM	HANN	HSVM
R	0.22	0.862	0.492	0.88
RMSE	6.01	1.361	3.861	1.36
NMSE	16.97	0.83	5.96	0.68
2 months ahead prediction				
R	0.14	0.71	0.29	0.72
RMSE	7.49	2.01	5.16	1.94
NMSE	27.00	1.32	11.63	1.17

4.3 Groundwater Condition with Urbanization

Change in groundwater level was investigated utilizing water level record of 22 wells during 2010 and 2015 which shows considerable decline in the levels (Fig. 10 (a)). Groundwater decline in the study area ranges from 5 to 37 m bgl (below ground level) where the decline is highest at Chikkabanavar and Sarjapura locations, as highlighted in red color on the map. Whereas, increase in water levels were also observed at some locations in the Southern part of the study area. The urbanization could be a major cause behind the depleting groundwater mainly because urbanization has led to increased groundwater pumping due to increased water demand. Although the water needs of the city is mainly met by surface water imported from the Cauvery River, it has been unable to catch up with the increasing water demand due to rapid population growth and expansion of the city. As a result, groundwater satisfies a large

proportion of current water need. Further, increased impervious surface, which is associated with urbanization, has led to decreased groundwater recharge in the area. Figure 10 (b) shows the impervious surface fractions within 30 m × 30 m grids derived using Landsat image (Fig. 10 (b)). The comparison of groundwater change map and the impervious surface map shows that the higher declines are not at the urban centre, but towards the urban periphery. This is mainly due to the fact the groundwater pumping is happening mainly at peri-urban areas (Sekhar et al., 2018). This also indicates that the dominating factor behind the decline in the study area is pumping as compared to decreased groundwater recharge due to urbanization. Furthermore, the decreased recharge could have been compensated by the leaking pipes and wastewater to some extent in the study area. The competitive demands of water from various sectors put additional pressure on groundwater resources. Kapetas et al. (2019) found that the increasing competition for water has led to a water deficit in the agricultural sector, an unmet environmental flow and a reduced capacity for urban supply during drought conditions. Therefore, to manage water resources where competitive demands co-exist, coordinated multi-level institutional relationships are important to improve water management practices and water allocations (Kapetas et al., 2019).

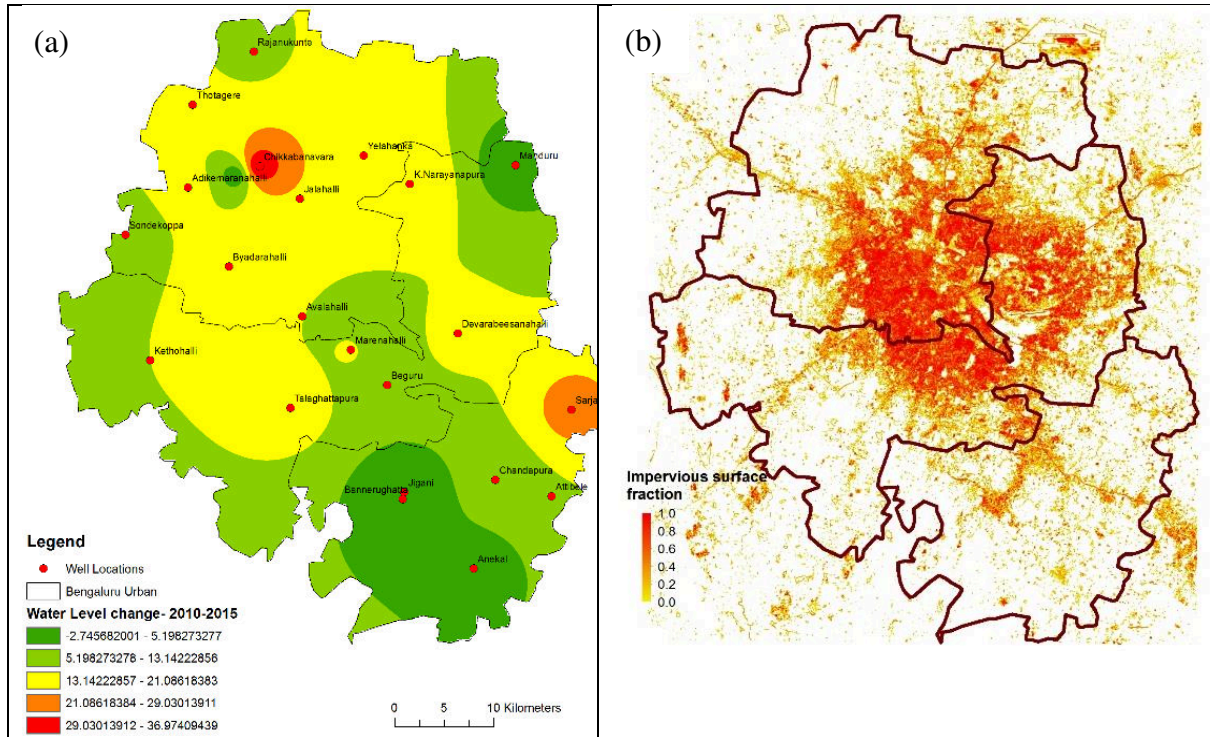


Fig. 10 Groundwater change map overlaid with observation wells (a) and impervious surface map (b). The values in map (b) shows the fraction of impervious surface within the 30 m × 30 m grids for the year 2010.

Though the hybrid HANN and HSVM models predicts the groundwater level fluctuations accurately, it does not give information about the corresponding physical processes in the aquifer. Further, the impact of additional input variables such as groundwater recharge from pipes leakage/sewers/drains has not been included in this study which could help in reducing the prediction error. Therefore, there are environments and applications for which each model type excels. In future studies, the methodology can be improved further by considering more advanced and efficient machine learning techniques, like deep algorithms, random forest, etc. Further, there is a scope in optimizing the number of parameters using other advanced optimization approaches.

5. Conclusion

In this study, we proposed an ensemble machine learning based modelling approach using input data pre-processing for prediction of groundwater level fluctuations. The developed approach was applied and assessed for monthly groundwater level prediction at an densely populated urban city (Bengaluru) in India. The selected area has been under severe water stress and groundwater table has declined significantly in last 10 years due to urbanization and heavy pumping. The hybrid models (HANN and HSVM) perform better than the original models (ANN and SVM) while predicting groundwater level fluctuations. It was also found that prediction accuracy decreases as we increase the time lead for both original and hybrid models.

It is interesting to observe that the population growth rate provided positive information and captured the impact of urbanization on the groundwater level fluctuations. Further, analysis of groundwater level decline (2010-2015) along with impervious surface suggest that the reason for declining trend in groundwater of urban centers is increased groundwater pumping rather than the decreased groundwater recharge due to urbanization. The results obtained from this study would be useful in identifying the causes for groundwater decline in urban centers under various climatic conditions. The developed approach would be useful particularly in the urban areas where physical based modelling is challenging due to scarcity of pipeline leakage or sewage/drainage line leakage data.

Acknowledgement

This study was supported by National Postdoctoral Fellowship (NPDF) grant (PDF/2017/000415) funded by Science and Engineering Research Board (SERB), India. The authors would like to acknowledge the District Groundwater Office, Groundwater Directorate Bengaluru, Karnataka for supplying the data.

Conflict of Interest

None

Data availability statement

The data used in the study can be provided on request by first author.

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Yadav, Basant; Gupta, Pankaj Kumar; Patidar, Nitesh; Himanshu, Sushil Kumar

2019-11-24

Elsevier

<https://doi.org/10.1016/j.scitotenv.2019.135539>

Yadav B, Gupta PK, Patidar N, Himanshu SK. (2020) Ensemble modelling framework for groundwater level prediction in urban areas of India. Science of the Total Environment, Volume 712, April 2020, Article number 135539