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2 Monte Carlo simulation of parameter confidence intervals for non-  
3 linear regression analysis of biological data using Microsoft Excel

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## 21   **Abstract**

22

23   This study describes a method to obtain parameter confidence intervals from the fitting of  
24   non-linear functions to experimental data, using the SOLVER and Analysis ToolPaK Add-  
25   In of the Microsoft Excel spreadsheet. Previously we have shown that Excel can fit  
26   complex multiple functions to biological data, obtaining values equivalent to those returned  
27   by more specialized statistical or mathematical software. However, a disadvantage of  
28   using the Excel method was the inability to return confidence intervals for the computed  
29   parameters or the correlations between them. Using a simple Monte-Carlo procedure  
30   within the Excel spreadsheet (without recourse to programming), SOLVER can provide  
31   parameter estimates (up to 200 at a time) for multiple 'virtual' data sets, from which the  
32   required confidence intervals and correlation coefficients can be obtained. The general  
33   utility of the method is exemplified by applying it to the analysis of the growth of *Listeria*  
34   *monocytogenes*, the growth inhibition of *Pseudomonas aeruginosa* by chlorhexidine and  
35   the further analysis of the electrophysiological data from the compound action potential of  
36   the rodent optic nerve.

37

## 38    **1    Introduction**

39

40    We have previously described the use of the Microsoft Excel spreadsheet to conduct non-  
41    linear regression (NLR) analysis of biological data [1]. Direct fitting of the dose response  
42    curve, for example, through the use of NLR techniques has been widely advocated, but  
43    access to, and comprehension of, commercial software are often at odds with the direct  
44    needs of the researcher. We recognised the ease of access and understanding that most  
45    researchers have of Microsoft Excel [2], which could allow even those with an elementary  
46    understanding of the spreadsheet to conduct relatively sophisticated data analyses,  
47    without the expense of purchasing and learning a new statistical or advanced  
48    mathematical package.

49

50    The SOLVER Add-In package of Excel allows the user to conduct investigations of non-  
51    linear (NL) functions using the minimization of the sum of squares of the errors between  
52    the observed and modelled values [1]. We further described the use of the technique for  
53    the modelling of multiple Gaussian functions, which described the observed  
54    electrophysiological data from the compound action potential of the rodent optic nerve [3].  
55    One particular failing of the SOLVER package was the inability to return parameter  
56    confidence intervals. It was noted that this requires the use of the Hessian matrix, whose  
57    calculation and use would invalidate the aim of making NLR open to anyone [1]. Hence the  
58    error analysis of the modelled and observed data was terminated at the calculation of the  
59    standard error of the fit.

60

61 Confidence intervals can be calculated from knowledge of the Hessian but can also be  
62 estimated using either the Bootstrap technique of re-sampling errors between the  
63 modelled fit and the observed, or from Monte-Carlo (MC) simulation [6]. The MC technique  
64 uses the standard error of the fit of the non-linear model to the observed data to produce  
65 sets of 'virtual' data. These data are modelled using the same non-linear model and a new  
66 group of parameters obtained for each virtual set. From the statistical distribution of these  
67 parameters, confidence intervals as well as correlation coefficients can be obtained.

68

69 We describe here the use of NLR within the Excel environment and augment our original  
70 method with a simple MC analysis, and show its general utility by applying it to analyse the  
71 growth of *Listeria monocytogenes*, the growth inhibition of *Pseudomonas aeruginosa* by  
72 chlorhexidine and the further analysis of the electrophysiological data from the compound  
73 action potential of the rodent optic nerve.

74

## 75    **2   Computational Methods and Theory**

76

77    For a given data set and a particular model ( $y_{fit}$ ), the sum of squares of the errors is given  
78    by

79    
$$SSE = \sum_{i=1}^n (y_i - y_{fit})^2$$

80    In a regression analysis the value of SSE is minimised by changing the parameter values  
81    of the model  $y_{fit}$ , resulting in the best estimates of these parameters. In linear regression  
82    this is solved analytically, but if using non-linear regression this is carried out numerically,  
83    based on the input of initial parameter estimates. The square root of the mean of the  
84    square of the error (RMSE) is the standard error of the fit. For a given set of conditions the  
85    model will return the expected value of  $y_i$ ,  $E(y_i) = \hat{y}_i$ . With linear regression, if all the  
86    prerequisite conditions are met, then the reported 95% confidence intervals will contain the  
87    true value of the regression parameters 95% of the time. With non-linear regression  
88    confidence intervals are found using linear approximations and the labelled 95%  
89    confidence intervals may not contain the true interval as often.

90

91    If the conditions required for regression are met, e.g. constant variance of error  
92    (homoscedasticity), normal distribution of errors, then the RMSE is an unbiased estimator  
93    of the standard deviation of the fit. A virtual data set can be calculated by adding random  
94    error to the expected value of  $y$ ;

95    
$$Y'_i = \hat{y}_i + N(0, RMSE)$$

96 This virtual data set can be analysed by NLR to give another set of parameters (the best fit  
97 estimates for this virtual data set).

$$98 \quad SSE = \sum_{i=1}^n (Y'_i - y_{fit})^2$$

99 Another set of virtual data can be generated and the NLR fitting repeated. In the procedure  
100 outlined here the sum of squares of the errors from multiple data sets are summed and the  
101 fitting of  $m$ -sets of data are conducted simultaneously

$$102 \quad SSE_{total} = \sum_{j=1}^m \sum_{i=1}^n (Y'_i - y_{fit})^2$$

103 From the  $m$ -sets of parameters obtained, frequency analyses of the parameter values are  
104 performed and the 95% confidence intervals obtained from the normal quantiles;  
105 covariance between parameter pairs can be found by calculating the parameters'  
106 correlation coefficient.

107

## 108 **2.1 FITTING THE MODIFIED GOMPERTZ EQUATION TO MICROBIAL GROWTH DATA**

109 The modified Gompertz equation is a standard empirical model for the fitting of microbial  
110 growth data [5].

$$111 \quad \log N(t) = A + C \exp\{-\exp(B(M - t))\} \quad (1)$$

112 Where  $A$  is the asymptotic number ( $\log \text{cfu ml}^{-1}$ ) as  $t$  tends to negative infinity,  $A+C =$   
113 maximum population density as  $t$  tends to positive infinity,  $B$  is a measure of the slope and  
114  $M$  is the time of maximum slope. From these fitted parameters the growth rate and lag are  
115 calculated, respectively, as

$$116 \quad \text{CB}/\exp(1) \quad (2)$$

$$117 \quad M-1/B \quad (3)$$

118 Data for the growth of *Listeria monocytogenes* at 30°C in growth media (Tryptone Soya  
119 broth) containing 9% salt in terms of log cfu ml<sup>-1</sup> over a period of 100 hours were obtained.

## 120 **2.2 FITTING THE LAMBERT-PEARSON MODEL TO MICROBIAL GROWTH INHIBITION DATA**

121 The time taken for a microbial culture to reach a specific optical density (also known as the  
122 time to detection, TTD) in the presence of an inhibitor is dependent on the concentration  
123 and dose response of that inhibitor. The Lambert-Pearson model (LPM, equation 4) [4]  
124 describes the visual growth of a culture as an exponential decay function of the  
125 concentration of the applied inhibitor. A plot of the log concentration against the relative  
126 rate to detection (RRTD, the ratio of the time to detection of the uninhibited culture, or  
127 positive control, to the time to detection of the test culture) gives a characteristic sinusoid,  
128 with inflexion at  $RRTD = 1/\exp(1)$ . A linear extrapolation from this point to the log  
129 concentration axis allows the estimation of the minimum inhibitory concentration (MIC,  
130 equation 5), and a linear extrapolation to the  $RRTD = 1$  axis allows the estimation of the  
131 non-inhibitory concentration (NIC, equation 6), the concentration below which normal

132 visual growth is observed even in the presence of the inhibitor.

$$133 \quad RRTD = \begin{cases} \text{if} & [x] = 0, & 1 \\ \text{else if} & [x] < [P_1] \\ \text{then} & \exp\left(-\left(\frac{[x]}{P_1}\right)^{P_2}\right) \\ \text{else if} & \frac{1}{e}(1 - P_2(\ln[x] - \ln P_1)) < 0, & 0 \\ \text{else} & \frac{1}{e}(1 - P_2(\ln[x] - \ln P_1)) \end{cases} \quad (4)$$

134 Where RRTD = relative rate to detection,  $[x]$  is the concentration of the given inhibitor,  $P_1$   
 135 is the concentration of inhibitor giving a relative inhibition of  $1/e$ , where  $e$  is the exponential  
 136 of 1, and  $P_2$  is a slope parameter which has been defined as the dose response due its  
 137 similarity with the Hill model.

138 Two biologically important parameters can be obtained from the LPM; the minimum  
 139 inhibitory concentration (MIC) and the non-inhibitory concentration (NIC) and are defined,  
 140 respectively, as

$$141 \quad MIC = P_1 \exp\left(\frac{1}{P_2}\right) \quad (5)$$

$$142 \quad NIC = P_1 \exp\left(\frac{1-e}{P_2}\right) \quad (6)$$

143 Data from the growth inhibition of *Pseudomonas aeruginosa* (ATCC 15442) in the  
 144 presence of chlorhexidine at 37°C was obtained using standard, published, methods  
 145 (Lambert and Pearson 2000).

146

### 147 **2.3 FURTHER ANALYSIS OF COMPOUND ACTION POTENTIAL OF THE RODENT OPTIC** 148 **NERVE**

149 The compound action potential from the rodent optic nerve typically has three peaks  
 150 (indicating the presence of three populations of axons with different conduction velocities)  
 151 with a rapidly decaying transient or artefact from the initial stimulus. Originally this  
 152 phenomenon was modelled using the sum of four Gaussian functions, one for each feature  
 153 of the CAP (Brown 2006).

$$154 \quad CAP = \sum_{i=1}^4 \frac{A_i}{w_i \sqrt{\pi/2}} \exp \left\{ -2 \left( \frac{t - c_i}{w_i} \right)^2 \right\} \quad (7)$$

156 where  $A_i$  is the area under the curve,  $w_i$  the width at half the maximum amplitude and  $c_i$  is  
 157 the latency to the maximum amplitude of peak  $i$ . This equation models the artefact as a  
 158 Gaussian; a secondary model which has some desirable features as described in this  
 159 report, models the artefact as a simple decay, modelling from the initial recording time of  
 160 1.04 ms.

$$161 \quad CAP = D_1 \exp(-D_2(t - 1.04)) \sum_{i=1}^3 \frac{A_i}{w_i \sqrt{\pi/2}} \exp \left\{ -2 \left( \frac{t - c_i}{w_i} \right)^2 \right\} \quad (8)$$

162 Where  $D_1$  and  $D_2$  are parameters describing the decay of the initial stimulus.

### 163   **3   Program description and sample runs**

164   The method can be split into 3-stages: Stage 1 fits the given NL model to the observed  
165   data using SOLVER. This generates the initial best fit parameters and the RMSE value of  
166   the fit. Stage 2 uses the RMSE to generate a set of random numbers based on  
167    $N(0, \text{RMSE})$ , which are added to the predicted data from Stage 1. The NL model is then  
168   applied to multiple virtual data sets simultaneously (using SOLVER) to generate multiple  
169   values of best-fit parameters. In stage 3 these values are statistically analysed to provide  
170   the mean of the best-fit parameters, their standard errors, 95% confidence intervals and  
171   parameter correlations. The data can also be used to provide confidence intervals for  
172   parameters calculated from the regressed parameters, which are often dependent on the  
173   magnitude of the correlation between those parameters.

#### 174   **3.1   NLR: EXCEL ANALYSIS OF THE GROWTH OF LISTERIA MONOCYTOGENES AT 30°C** 175       **IN HIGH SALT MEDIA**

##### 176   **3.1.1   Monte-Carlo: Excel Analysis**

177   Stage 1. The initial part of the procedure generally follows that given previously [3] except  
178   in this case the modified Gompertz model (1) was used. The data used and the initial NLR  
179   are shown in [Figure 1](#). The sum of the squares of the errors (SSE, Cell E39) was  
180   calculated using the inbuilt “SUMXMY2(data range 1,data range 2)”, where the first data  
181   range was the modelled values and the second data range was the observed values. Cell  
182   E41 divides this by the degrees of freedom (Cell E40) and takes the square root to give  
183   the root mean square error (RMSE). This is the standard error of the curve fit. The

184 SOLVER Package was used to minimise this value, by changing the values of the four  
185 parameters A, C, B and M. [Figure 2](#) shows a plot of the observed data and the modelled  
186 function.

187

188 *Stage 2. Generation of random numbers with a distribution of  $N(0, RMSE)$ :* (It is assumed  
189 the user has installed the Analysis ToolPak Add-In). On a separate worksheet, the  
190 Random Number Generator was used to generate an array of 50 columns of 33 random  
191 numbers using the RMSE of the fitted model as the standard deviation ([Figure 3](#)). The  
192 number of columns used is set by the maximum number of values that SOLVER can  
193 handle (200) divided by the number of parameters in the model. A random seed number of  
194 2 was used for illustrative purposes as the use of this seed number will allow any reader to  
195 recreate the exact procedure carried out here.

196

197 *Generation of virtual data:* The random data was added to the modelled log cfu ml<sup>-1</sup> data to  
198 produce a set of 50 virtual observed data. On the spreadsheet these were conveniently  
199 located below the random number array.

200

201 *Stage 3. Fitting multiple models simultaneously using SOLVER:* Below each set of virtual  
202 data the modified Gompertz model was entered ([Figure 4](#)). The regression parameters  
203 were placed below this: the initial parameters for each set used the parameters from the  
204 initial model fit, although it is advised to check that the parameters do not represent a local  
205 rather than the global minimum). The SSE between the virtual data and the modelled data  
206 was calculated per data set (Cells C115 to AZ115). The SSE from each data set was

207 summed and this total value placed in cell C117; SOLVER was used to minimise this total  
208 SSE by changing all the 200 parameters concurrently. This procedure gave 50 sets of  
209 modelled parameters per run. A target SSE of 50 times the SSE obtained from the initial fit  
210 (cell B118) was used to monitor the progress of the fitting.  
211 After the minimization procedure, from the fitted parameters the mean and standard  
212 deviations were found. The 95% confidence intervals were calculated from the 95%  
213 percentiles using the syntax '=PERCENTILE(array, 0.025)', and '=PERCENTILE(array,  
214 0.975)'. The correlation coefficient was found using the "CORREL(data range 1, data range  
215 2)" function. [Tables 1a](#) and [1b](#) give the results of this MC analysis.

216

### 217 **3.1.2 Calculation of Biological Parameters**

218 The growth rate, maximum population density and the lag before the onset of growth are  
219 important biological parameters and have to be calculated from the parameters obtained  
220 from the fitting of the modified Gompertz. However, a singular problem is the calculation of  
221 the confidence interval of the calculated parameter. For example the MPD = A + C, but the  
222 variance is given by

$$Var(A + C) = Var(A) + Var(C) + 2Cov(AC)$$

223 Knowledge of the correlation between parameters allows the covariance to be calculated.  
224 However in more complex cases such as the calculation of the growth rate ( given by  
225  $BC/e$ ), the calculation of the confidence interval becomes complex. The confidence  
226 intervals for these biological parameters, however, can be estimated from the parameter  
227 data of the MC analysis. For each parameter set the particular biological parameter was

228 calculated, giving 101 values (including the original fitting parameters).From these values  
229 the required percentiles were calculated. In this particular case a re-parameterized  
230 version of the modified Gompertz [5] was used to show that the ranges obtained by  
231 running a non-linear analysis using JMP were equivalent to those obtained directly from  
232 the MC analysis ([Table 2](#)).

233

## 234 4 Samples of Program Runs

### 235 4.1 INHIBITION OF PSEUDOMONAS AERUGINOSA BY CHLORHEXIDINE

236 The LPM (Eqn. 4) can be written in Excel as a nested series of IF-statements (e.g. see  
237 [Figure 6](#)). Initial estimates for the regression parameters can be obtained from an analysis  
238 of a plot of the chlorhexidine concentration against the RRTD ([Figure 5](#)). Using SOLVER  
239 estimates for parameters P1 and P2 and the RMSE were obtained. The fitted parameters  
240 and the RMSE were used to prime the MC analysis. The results of the Excel MC analysis  
241 are given in [Table 3](#) and [Figure 6](#) shows the spreadsheet used.

242

243 A table (81x100) of random numbers based on  $N(0, \text{RMSE})$  was produced (cells C4 to  
244 CX84). These random numbers were added to the modelled values (cells C88 to CX168),  
245 and the non-linear fitting repeated (C172 to CX252) by regressing all 200 parameters at  
246 once (Cells C255 to CX256). [Figure 6](#) shows a portion of the calculation performed. Cell  
247 C259 sums the SSE for each regression performed (cells C258 to CX258). Cells B262 to  
248 CX262 and C263 to CX263 calculate the MIC and NIC values from the regressed  
249 parameters respectively.

250

## 251 4.2 FURTHER ANALYSIS OF COMPOUND ACTION POTENTIAL OF THE RODENT OPTIC

### 252 NERVE

253 The stimulus-evoked compound action potential from the mouse optic nerve was  
254 successfully modelled using multiple Gaussian functions (Brown 2006). The original work  
255 used four Gaussian functions to simulate the three peaks of the CAP and the brief stimulus  
256 artefact (Eqn.7). This model was set up in Excel and the 16 parameters regressed. The  
257 sum of squares obtained was 0.09987; the parameter values for Peaks 1,2 and 3 were  
258 essentially identical to those published (nb., a typographical error in the publication gave  
259 the area of peak 1 as 7.663, whereas it should have read 0.633). The estimated parameter  
260 values for the artefact were, however, different from those published. The peak area found  
261 in this analysis was 5.577 vs. 7.180 found previously and a calculated amplitude of 30.8  
262 vs. 38.042.

263  
264 The standard error of the fit (0.02986) was used to produce an array (96 x124) of normally  
265 distributed random numbers. These values were added to the modelled data (on a  
266 separate Excel sheet) to produce 96 virtual data sets (Cells DH5 to GY128), [Figure 7](#). (nb  
267 columns and rows have been 'hidden' to show the full sheet). The model was added to  
268 each cell M5 to DD128, the parameters were placed below each set of modelled data:  
269 cells M132 to DD143. The calculated SSE between the modelled data and their respective  
270 virtual data set was placed in cells M145 to DD145. The sum of these SSE was calculated  
271 in Cell L146. Due to the SOLVER limit of 200 parameters, the MC analysis had to be done  
272 in batches of 16. The results of the Monte-Carlo analysis (96 runs; 6 runs of 16) are given

273 in [Table 4a](#). The values obtained for the parameters are very similar to that previously  
274 published, apart for the values for the artefact. The confidence interval for the area of the  
275 artefact ranged from 4 to 10.7 and all correlations between parameters A4, w4 and c4 had  
276 magnitudes greater than 0.994, suggesting that the model was over-parameterized.

277

278 A NLR analysis using the JMP statistical package gave an estimate for A4 of 5.5788 (95%  
279 CI of 2.595 – 21.835), and correlations greater than 0.994 between A4, w4 and c4.

280

281 In a second Excel MC study, the artefact was modelled by a simple exponential decay,  
282 replacing the Gaussian for the artefact by the function  $D_1 \text{Exp}(-D_2(t-1.04))$ . A similar MC  
283 analysis was undertaken; the parameter estimates found for the three principal peaks  
284 were relatively unchanged, but the parameter estimates for the artefact now had narrower  
285 confidence intervals and the correlation between D1 and D2 = 0.246 ([Table 4b](#))

#### 286 **4.3 CAVEATS TO USING MC ANALYSIS WITHIN EXCEL**

287 The MC analysis within Excel is initially primed using the parameter estimates from the  
288 initial SOLVER minimisation procedure. It is possible that the estimates relate not to a  
289 global minimum but to a local minimum, especially if there is a high degree of correlation  
290 between given parameters (as was observed in the first analysis of the CAP data). One  
291 method to overcome any such possibility is to use different initial parameter estimates for  
292 each virtual dataset. This can be done using Excel's "RANDBETWEEN(a,b)" function,  
293 where the user generates a scaled value of a parameter between two integer extrema (a  
294 and b), and rescales to accommodate the desired magnitude of the initial parameter.

295

#### 296 **4.4 COMPARISON OF THE EXCEL NLR AND MC ANALYSIS WITH *MATHEMATICA***

297 The non-linear regression capability of *JMP* was used to fit the three sets of sample data;  
298 Tables 1, 2, 3, and 4c give the parameters, and their confidence intervals obtained using  
299 this sophisticated software; Table 1b also compares the parameter correlations obtained  
300 between the Excel MC and JMP NLR analysis. A small program was written to conduct a  
301 Monte-Carlo analysis within *Mathematica* (Version 8) with the subsequent analysis of  
302 10,000 virtual data sets (approx 2 to 5 minutes per 10,000 runs) for each of the fitted  
303 models. The results of these MC analyses are also given in Tables 1a, 3, and 4d. The NLR  
304 analysis using *JMP* essentially gave the same parameter estimates as that from the NLR  
305 Excel analysis; the confidence intervals calculated using the Excel MC technique closely  
306 agree with those calculated using the Hessian method within *JMP*. A comparison of the  
307 results of the MC analysis of *Mathematica* also compares well with the Excel output. It  
308 should be noted that the confidence intervals obtained from the MC analysis and the direct  
309 NLR analysis using *JMP* do not completely agree with each other and this simply reflects  
310 the differences in the techniques used. Each is equally correct.

311

312 The comparison between the parameter estimates and their confidence intervals as  
313 obtained from the Excel MC analysis with either the direct NLR or the MC analyses using  
314 *JMP* or *Mathematica* demonstrates the capacity of Excel to produce results equivalent to  
315 those from more sophisticated packages.

## 316 **5 Hardware and software specification**

317

318 The method was carried out on a basic desktop computer with an AMD Phenom 9750  
319 Quad core processor (2.4GHz), using Microsoft Excel 2007 under Windows 7. Non linear  
320 regression comparisons were carried out using the JMP (4.0.4) Statistical Software (SAS  
321 Institute Inc, Cary NC) and Monte-Carlo comparisons were carried out using *Mathematica*  
322 Version 8.0.0.0 (Wolfram Research Inc, Champaign IL, USA).

323

324

325

## 326    **6   Program availability**

327    Spreadsheets with the worked examples are available from the author on request. The  
328    *Mathematica* coding used to produce the NLR fits and Monte-Carlo simulations are also  
329    available from the corresponding author.

330

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350

351

352 **Tables**

353

354 **Table 1a.** Excel MC (100 iterations), JMP (non-linear regression) and *Mathematica* MC  
 355 (10,000 iterations) analyses for the fitting of the modified Gompertz equation to *Listeria*  
 356 *monocytogenes* growth data

| Method                | Parameter | Estimate | StdErr | LCL    | UCL    |
|-----------------------|-----------|----------|--------|--------|--------|
| Excel MC              | A         | 3.948    | 0.0278 | 3.906  | 3.999  |
|                       | C         | 4.896    | 0.0520 | 4.801  | 4.977  |
|                       | B         | 0.095    | 0.0033 | 0.090  | 0.101  |
|                       | M         | 30.318   | 0.2617 | 29.766 | 30.792 |
| JMP NLR               | A         | 3.951    | 0.0279 | 3.892  | 4.008  |
|                       | C         | 4.900    | 0.0486 | 4.802  | 5.000  |
|                       | B         | 0.095    | 0.0033 | 0.089  | 0.102  |
|                       | M         | 30.341   | 0.2858 | 29.738 | 30.937 |
| <i>Mathematica</i> MC | A         | 3.95     | 0.0279 | 3.895  | 4.0048 |
|                       | C         | 4.9003   | 0.0481 | 4.807  | 4.995  |
|                       | B         | 0.095    | 0.0033 | 0.089  | 0.102  |
|                       | M         | 30.340   | 0.2833 | 29.776 | 30.882 |

357 Units: A and C:  $\log_{10}\text{cfu ml}^{-1}$ ; B: 1/hr M: hr

358 **Table 1b. Parameter Correlation Table Obtained using Excel MC**  
 359 **and JMP NLR analysis (brackets)**

|   | A                  | C                  | B                 | M |
|---|--------------------|--------------------|-------------------|---|
| A | 1                  |                    |                   |   |
| C | -0.697<br>(-0.675) | 1                  |                   |   |
| B | 0.347<br>(0.357)   | -0.658<br>(-0.650) | 1                 |   |
| M | 0.546<br>(0.499)   | -0.135<br>(-0.088) | 0.0122<br>(0.161) | 1 |

360

361

362 **Table 2. Calculation of Biological Parameters from the modified Gompertz using**  
 363 **Excel MC, compared to the JMP NLR fitting of the re-parameterised modified**  
 364 **Gompertz equation for the growth of *Listeria monocytogenes* at 30°C in high salt**  
 365 **(9%).**

| Method   | Parameter   | Estimate | StdErr | LCL    | UCL    |
|----------|-------------|----------|--------|--------|--------|
| Excel MC | Growth rate | 0.172    | 0.005  | 0.162  | 0.182  |
|          | Lag         | 19.806   | 0.470  | 18.733 | 20.589 |
|          | MPD         | 8.845    | 0.039  | 8.765  | 8.918  |
| JMP NLR  | Growth rate | 0.171    | 0.005  | 0.162  | 0.182  |
|          | Lag         | 19.829   | 0.499  | 18.765 | 20.878 |
|          | MPD         | 8.850    | 0.036  | 8.778  | 8.924  |

366 Units: Growth rate:  $\log_{10} \text{ cfu ml}^{-1} \text{ hr}^{-1}$ ; lag: hrs; MPD  $\log_{10} \text{ cfu ml}^{-1}$   
 367

368 **Table 3. Excel MC (100 iterations), JMP (non-linear regression) and *Mathematica***  
369 **MC(10,000 iterations) analyses for the fitting of the LPM to the inhibition of**  
370 ***Pseudomonas aeruginosa* in the presence of chlorhexidine.**

| Method                | Parameter | Estimate | StdErr | LCL   | UCL   |
|-----------------------|-----------|----------|--------|-------|-------|
| Excel MC              | P1        | 7.265    | 0.093  | 7.109 | 7.455 |
|                       | P2        | 1.150    | 0.022  | 1.107 | 1.187 |
| JMP NLR               | P1        | 7.257    | 0.085  | 7.092 | 7.430 |
|                       | P2        | 1.149    | 0.019  | 1.114 | 1.185 |
| <i>Mathematica</i> MC | P1        | 7.257    | 0.085  | 7.095 | 7.427 |
|                       | P2        | 1.149    | 0.019  | 1.113 | 1.186 |
| Excel MC              | MIC       | 17.34    | 0.428  | 16.61 | 18.18 |
|                       | NIC       | 1.630    | 0.044  | 1.550 | 1.709 |
| <i>Mathematica</i> MC | MIC       | 17.333   | 0.372  | 16.62 | 18.09 |
|                       | NIC       | 1.626    | 0.037  | 1.554 | 1.698 |

371 Units; P1, MIC and NIC (mg/l); P2 dimensionless.  
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**Table 4a. Excel MC (96 iterations) analysis of CAP data (Eqn. 7)**

| Peak     | Parameter | Estimate | Stdev | LCL   | UCL    |
|----------|-----------|----------|-------|-------|--------|
| Pk1      | A1        | 0.633    | 0.007 | 0.620 | 0.648  |
|          | w1        | 0.243    | 0.002 | 0.238 | 0.247  |
|          | c1        | 1.397    | 0.001 | 1.394 | 1.398  |
| Pk2      | A2        | 1.552    | 0.017 | 1.517 | 1.579  |
|          | w2        | 0.418    | 0.004 | 0.410 | 0.423  |
|          | c2        | 1.875    | 0.001 | 1.872 | 1.877  |
| Pk3      | A3        | 1.288    | 0.013 | 1.262 | 1.313  |
|          | w3        | 0.609    | 0.006 | 0.598 | 0.621  |
|          | c3        | 2.566    | 0.004 | 2.559 | 2.574  |
| Artefact | A4        | 8.214    | 2.675 | 4.002 | 10.697 |
|          | w4        | 0.152    | 0.009 | 0.135 | 0.162  |
|          | c4        | 0.883    | 0.021 | 0.863 | 0.920  |

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**Table 4b: Excel MC analysis (96 iterations) of CAP data (Eqn. 8)**

| Peak     | Parameter | Estimate | Stdev | LCL    | UCL    |
|----------|-----------|----------|-------|--------|--------|
| Pk1      | A1        | 0.621    | 0.008 | 0.606  | 0.636  |
|          | w1        | 0.238    | 0.002 | 0.234  | 0.243  |
|          | c1        | 1.397    | 0.001 | 1.394  | 1.399  |
| Pk2      | A2        | 1.564    | 0.019 | 1.522  | 1.595  |
|          | w2        | 0.421    | 0.005 | 0.411  | 0.427  |
|          | c2        | 1.874    | 0.002 | 1.871  | 1.877  |
| Pk3      | A3        | 1.283    | 0.015 | 1.254  | 1.313  |
|          | w3        | 0.607    | 0.007 | 0.596  | 0.621  |
|          | c3        | 2.568    | 0.004 | 2.559  | 2.577  |
| Artefact | D1        | 4.996    | 0.034 | 4.928  | 5.058  |
|          | D2        | 30.906   | 0.194 | 30.447 | 31.455 |

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**Table 4c: JMP NLR analysis of CAP data (Eqn. 8)**

| Peak     | Parameter | Estimate | ApproxStdErr | LCL    | UCL    |
|----------|-----------|----------|--------------|--------|--------|
| Pk1      | A1        | 0.620    | 0.009        | 0.603  | 0.637  |
|          | w1        | 0.238    | 0.003        | 0.233  | 0.243  |
|          | c1        | 1.396    | 0.001        | 1.394  | 1.399  |
| Pk2      | A2        | 1.566    | 0.019        | 1.529  | 1.603  |
|          | w2        | 0.421    | 0.004        | 0.413  | 0.430  |
|          | c2        | 1.874    | 0.002        | 1.871  | 1.877  |
| Pk3      | A3        | 1.281    | 0.015        | 1.252  | 1.312  |
|          | w3        | 0.607    | 0.007        | 0.593  | 0.621  |
|          | c3        | 2.568    | 0.004        | 2.560  | 2.576  |
| Artefact | D1        | 4.997    | 0.034        | 4.931  | 5.063  |
|          | D2        | 30.907   | 0.414        | 30.124 | 31.712 |

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**Table 4d: *Mathematica* MC (10,000 iterations) analysis of CAP data (Eqn. 8)**

| Peak     | Parameter | Estimate | ApproxStdErr | LCL    | UCL    |
|----------|-----------|----------|--------------|--------|--------|
| Pk1      | A1        | 0.621    | 0.008        | 0.603  | 0.636  |
|          | w1        | 0.238    | 0.002        | 0.233  | 0.242  |
|          | c1        | 1.397    | 0.001        | 1.394  | 1.399  |
| Pk2      | A2        | 1.564    | 0.018        | 1.530  | 1.601  |
|          | w2        | 0.421    | 0.004        | 0.413  | 0.430  |
|          | c2        | 1.874    | 0.016        | 1.871  | 1.877  |
| Pk3      | A3        | 1.282    | 0.015        | 1.253  | 1.312  |
|          | w3        | 0.607    | 0.007        | 0.594  | 0.621  |
|          | c3        | 2.568    | 0.004        | 2.560  | 2.576  |
| Artefact | D1        | 4.997    | 0.034        | 4.931  | 5.063  |
|          | D2        | 30.925   | 0.413        | 30.141 | 31.752 |

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## 385    **Legends to Figures**

386

387    Figure 1. Non-linear regression analysis of the observed growth data for *Listeria*

388    *monocytogenes* at 30°C in 9% salt from an initial cellular density of  $7.586 \times 10^3$  cfu ml<sup>-1</sup>.

389    The growth was monitored over a 90 hour period. The observed numbers as their decimal  
390    log were modelled using the standard modified Gompertz equation [5].

391    Figure 2. Plot of the growth data of *L. monocytogenes* at 30°C in 9% salt (symbols) with  
392    the fitted modified-Gompertz model (line).

393    Figure 3. A portion of the (50 x 33) random number array generated using the random  
394    number feature of Excel's Analysis Addin with a distribution of N(0, 0.09047), using a  
395    random seed number of 2.

396    Figure 4. A portion of the (50 x 33) NLR array; column B reproduces the NLR fitting of the  
397    original data, with cells B111 to B114 reproducing the regressed parameters. Well C77  
398    shows the syntax used for the formula, which is reproduced over the array. Cells C115 to  
399    AZ115 calculate the SSE between the modelled data and the respective virtual data set.  
400    Cell B117 sums all the 50 individual SSE values. This value is then minimised using the  
401    SOLVER utility.

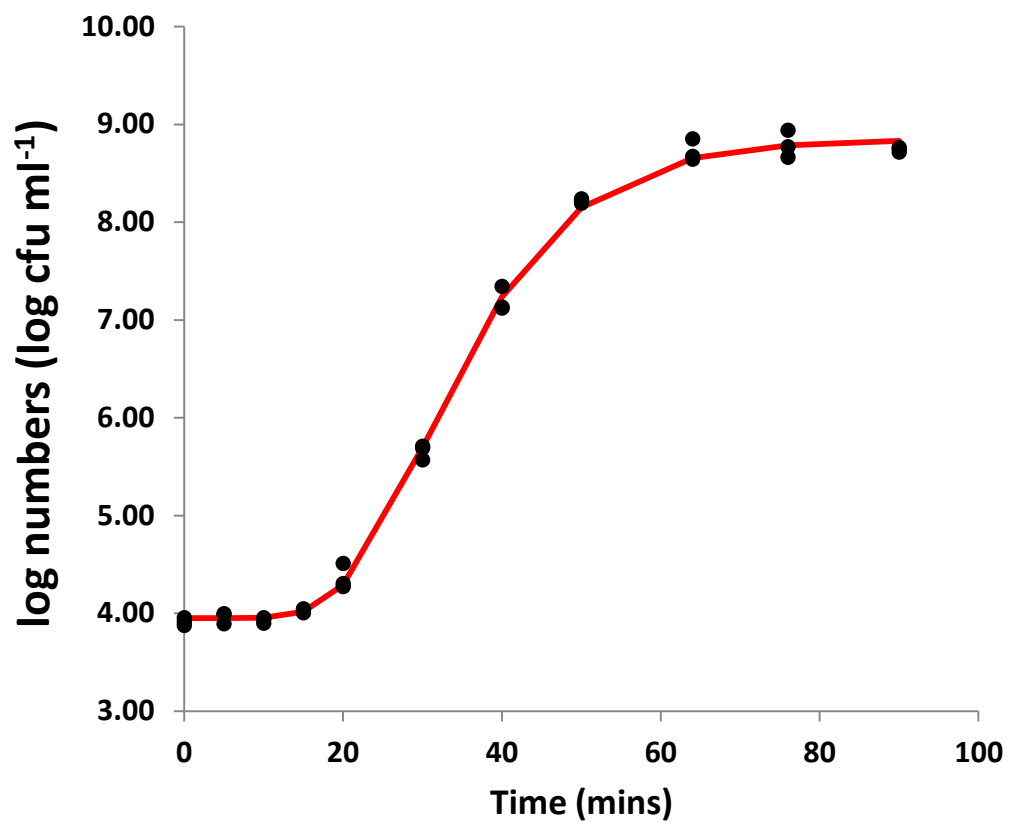
402    Figure 5. A plot of chlorhexidine concentration (mg l<sup>-1</sup>) against the observed relative rate to  
403    detection for the growth of *Pseudomonas aeruginosa* (ATCC 15442) in TSB at 37°C  
404    (symbols) and the fitted NLR model (line).

405    Figure 6. Spreadsheet used for the Excel MC analysis of the fitting of the LPM to the data  
406    for the growth inhibition of *Ps.aeruginosa* by chlorhexidine.

407 Figure 7. Spreadsheet used for the Excel MC analysis of the fitting of a multiple Gaussian  
408 function (Eqn. 7) to CAP data.  
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|    | A | B         | C        | D     | E        |
|----|---|-----------|----------|-------|----------|
| 1  |   |           |          |       |          |
| 2  |   |           |          |       |          |
| 3  |   | Obs       | Time/hr  | LogNo | Gompertz |
| 4  |   | 1         | 0        | 3.88  | 3.95     |
| 5  |   | 2         | 0        | 3.95  | 3.95     |
| 6  |   | 3         | 0        | 3.91  | 3.95     |
| 7  |   | 4         | 5        | 3.89  | 3.95     |
| 8  |   | 5         | 5        | 3.99  | 3.95     |
| 9  |   | 6         | 5        | 4.00  | 3.95     |
| 10 |   | 7         | 10       | 3.90  | 3.96     |
| 11 |   | 8         | 10       | 3.95  | 3.96     |
| 12 |   | 9         | 10       | 3.94  | 3.96     |
| 13 |   | 10        | 15       | 4.05  | 4.02     |
| 14 |   | 11        | 15       | 4.00  | 4.02     |
| 15 |   | 12        | 15       | 4.04  | 4.02     |
| 16 |   | 13        | 20       | 4.51  | 4.29     |
| 17 |   | 14        | 20       | 4.30  | 4.29     |
| 18 |   | 15        | 20       | 4.27  | 4.29     |
| 19 |   | 16        | 30       | 5.69  | 5.69     |
| 20 |   | 17        | 30       | 5.57  | 5.69     |
| 21 |   | 18        | 30       | 5.71  | 5.69     |
| 22 |   | 19        | 40       | 7.34  | 7.24     |
| 23 |   | 20        | 40       | 7.12  | 7.24     |
| 24 |   | 21        | 40       | 7.13  | 7.24     |
| 25 |   | 22        | 50       | 8.24  | 8.15     |
| 26 |   | 23        | 50       | 8.22  | 8.15     |
| 27 |   | 24        | 50       | 8.19  | 8.15     |
| 28 |   | 25        | 64       | 8.67  | 8.65     |
| 29 |   | 26        | 64       | 8.85  | 8.65     |
| 30 |   | 27        | 64       | 8.64  | 8.65     |
| 31 |   | 28        | 76       | 8.66  | 8.79     |
| 32 |   | 29        | 76       | 8.77  | 8.79     |
| 33 |   | 30        | 76       | 8.94  | 8.79     |
| 34 |   | 31        | 90       | 8.75  | 8.83     |
| 35 |   | 32        | 90       | 8.76  | 8.83     |
| 36 |   | 33        | 90       | 8.72  | 8.83     |
| 37 |   |           |          |       |          |
| 38 |   | Parameter | Estimate |       |          |
| 39 |   | A         | 3.951    | SSE   | 0.23882  |
| 40 |   | C         | 4.900    | DoF   | 29       |
| 41 |   | B         | 0.095    | RMSE  | 0.09075  |
| 42 |   | M         | 30.341   |       |          |



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416 Figure 2

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|    | A    | B         | C        | D        | E        | F        | G        | H            |
|----|------|-----------|----------|----------|----------|----------|----------|--------------|
| 1  |      |           |          |          |          |          |          |              |
| 2  | RMSE | 0.090747  |          |          |          |          |          |              |
| 3  |      |           |          |          |          |          |          |              |
| 4  |      |           |          |          |          |          |          |              |
| 5  |      | <b>no</b> | <b>1</b> | <b>2</b> | <b>3</b> | <b>4</b> | <b>5</b> | <b>6</b>     |
| 6  |      | <b>1</b>  | -0.27177 | 0.112094 | 0.057959 | 0.009818 | 0.116198 | 0.022917399  |
| 7  |      | <b>2</b>  | -0.0408  | 0.073162 | 0.027441 | 0.01999  | -0.00484 | -0.016152197 |
| 8  |      | <b>3</b>  | 0.013121 | 0.005853 | -0.04004 | -0.12229 | 0.121177 | 0.08340568   |
| 9  |      | <b>4</b>  | -0.13812 | -0.14519 | -0.03006 | 0.063873 | -0.0022  | -0.025016443 |
| 10 |      | <b>5</b>  | 0.074846 | 0.033108 | 0.040228 | -0.01283 | -0.03762 | -0.09728479  |
| 11 |      | <b>6</b>  | -0.11262 | -0.0679  | 0.155139 | 0.038026 | 0.108661 | 0.031230421  |
| 12 |      | <b>7</b>  | -0.03568 | -0.14927 | 0.053359 | -0.12548 | -0.07223 | 0.0336726    |
| 13 |      | <b>8</b>  | 0.154248 | 0.00085  | -0.0747  | -0.14346 | -0.09552 | 0.118928897  |
| 14 |      | <b>9</b>  | 0.084781 | -0.06085 | -0.0096  | -0.10539 | 0.011188 | 0.04305846   |
| 15 |      | <b>10</b> | -0.05888 | 0.084385 | -0.10152 | 0.116863 | 0.113325 | -0.030171924 |
| 16 |      | <b>11</b> | -0.06138 | 0.070147 | 0.207505 | 0.022917 | 0.031732 | 0.042074346  |
| 17 |      | <b>12</b> | -0.12809 | 0.049439 | 0.01095  | -0.09689 | 0.029607 | 0.245178551  |
| 18 |      | <b>13</b> | -0.00068 | -0.00305 | 0.086133 | -0.05195 | 0.056966 | 0.036319875  |
| 19 |      | <b>14</b> | -0.07968 | 0.219385 | 0.176514 | 0.026766 | -0.08762 | 0.099635975  |
| 20 |      | <b>15</b> | 0.127024 | 0.04708  | 0.056282 | 0.072245 | 0.004506 | 0.005210754  |

Figure 3

| ... X ✓ fx =C\$111+C\$112*EXP(-1*EXP(C\$113*(C\$114-\$A77))) |         |          |           |          |          |          |          |    |
|--------------------------------------------------------------|---------|----------|-----------|----------|----------|----------|----------|----|
|                                                              | A       | B        | C         | D        | E        | F        | G        |    |
| 76                                                           | Time/hr | MOD      | 1         | 2        | 3        | 4        | 5        |    |
| 77                                                           | 0       | 3.951    | =C\$111+C | 3.94     | 3.97     | 3.92     | 3.97     |    |
| 78                                                           | 0       | 3.951    | 3.91      | 3.94     | 3.97     | 3.92     | 3.97     |    |
| 79                                                           | 0       | 3.951    | 3.91      | 3.94     | 3.97     | 3.92     | 3.97     |    |
| 80                                                           | 5       | 3.951    | 3.91      | 3.94     | 3.97     | 3.92     | 3.97     |    |
| 81                                                           | 5       | 3.951    | 3.91      | 3.94     | 3.97     | 3.92     | 3.97     |    |
| 82                                                           | 5       | 3.951    | 3.91      | 3.94     | 3.97     | 3.92     | 3.97     |    |
| 83                                                           | 10      | 3.955    | 3.91      | 3.95     | 3.98     | 3.92     | 3.98     |    |
| 84                                                           | 10      | 3.955    | 3.91      | 3.95     | 3.98     | 3.92     | 3.98     |    |
| 85                                                           | 10      | 3.955    | 3.91      | 3.95     | 3.98     | 3.92     | 3.98     |    |
| 86                                                           | 15      | 4.017    | 3.98      | 4.03     | 4.06     | 4.00     | 4.04     |    |
| 87                                                           | 15      | 4.017    | 3.98      | 4.03     | 4.06     | 4.00     | 4.04     |    |
| 88                                                           | 15      | 4.017    | 3.98      | 4.03     | 4.06     | 4.00     | 4.04     |    |
| 89                                                           | 20      | 4.288    | 4.29      | 4.33     | 4.35     | 4.30     | 4.32     |    |
| 90                                                           | 20      | 4.288    | 4.29      | 4.33     | 4.35     | 4.30     | 4.32     |    |
| 91                                                           | 20      | 4.288    | 4.29      | 4.33     | 4.35     | 4.30     | 4.32     |    |
| 92                                                           | 30      | 5.695    | 5.77      | 5.69     | 5.71     | 5.69     | 5.74     |    |
| 93                                                           | 30      | 5.695    | 5.77      | 5.69     | 5.71     | 5.69     | 5.74     |    |
| 94                                                           | 30      | 5.695    | 5.77      | 5.69     | 5.71     | 5.69     | 5.74     |    |
| 95                                                           | 40      | 7.238    | 7.32      | 7.18     | 7.18     | 7.21     | 7.26     |    |
| 96                                                           | 40      | 7.238    | 7.32      | 7.18     | 7.18     | 7.21     | 7.26     |    |
| 97                                                           | 40      | 7.238    | 7.32      | 7.18     | 7.18     | 7.21     | 7.26     |    |
| 98                                                           | 50      | 8.150    | 8.20      | 8.11     | 8.09     | 8.13     | 8.15     |    |
| 99                                                           | 50      | 8.150    | 8.20      | 8.11     | 8.09     | 8.13     | 8.15     |    |
| 100                                                          | 50      | 8.150    | 8.20      | 8.11     | 8.09     | 8.13     | 8.15     |    |
| 101                                                          | 64      | 8.655    | 8.67      | 8.66     | 8.62     | 8.67     | 8.64     |    |
| 102                                                          | 64      | 8.655    | 8.67      | 8.66     | 8.62     | 8.67     | 8.64     |    |
| 103                                                          | 64      | 8.655    | 8.67      | 8.66     | 8.62     | 8.67     | 8.64     |    |
| 104                                                          | 76      | 8.787    | 8.79      | 8.82     | 8.77     | 8.81     | 8.76     |    |
| 105                                                          | 76      | 8.787    | 8.79      | 8.82     | 8.77     | 8.81     | 8.76     |    |
| 106                                                          | 76      | 8.787    | 8.79      | 8.82     | 8.77     | 8.81     | 8.76     |    |
| 107                                                          | 90      | 8.833    | 8.83      | 8.88     | 8.83     | 8.87     | 8.81     |    |
| 108                                                          | 90      | 8.833    | 8.83      | 8.88     | 8.83     | 8.87     | 8.81     |    |
| 109                                                          | 90      | 8.833    | 8.83      | 8.88     | 8.83     | 8.87     | 8.81     |    |
| 110                                                          |         |          |           |          |          |          |          |    |
| 111                                                          | A       | 3.951    | 3.907     | 3.944    | 3.973    | 3.917    | 3.973    |    |
| 112                                                          | C       | 4.900    | 4.940     | 4.959    | 4.876    | 4.973    | 4.852    |    |
| 113                                                          | B       | 0.095    | 0.097     | 0.090    | 0.090    | 0.092    | 0.095    |    |
| 114                                                          | M       | 30.341   | 29.726    | 30.463   | 30.383   | 30.321   | 30.115   |    |
| 115                                                          | sse     | 0.238816 | 0.253706  | 0.254936 | 0.303308 | 0.211335 | 0.115958 | 0. |
| 116                                                          |         |          |           |          |          |          |          |    |
| 117                                                          | Tot SSE | 11.55302 |           |          |          |          |          |    |
| 118                                                          | Targ    | 11.94079 |           |          |          |          |          |    |
| 119                                                          |         |          |           |          |          |          |          |    |

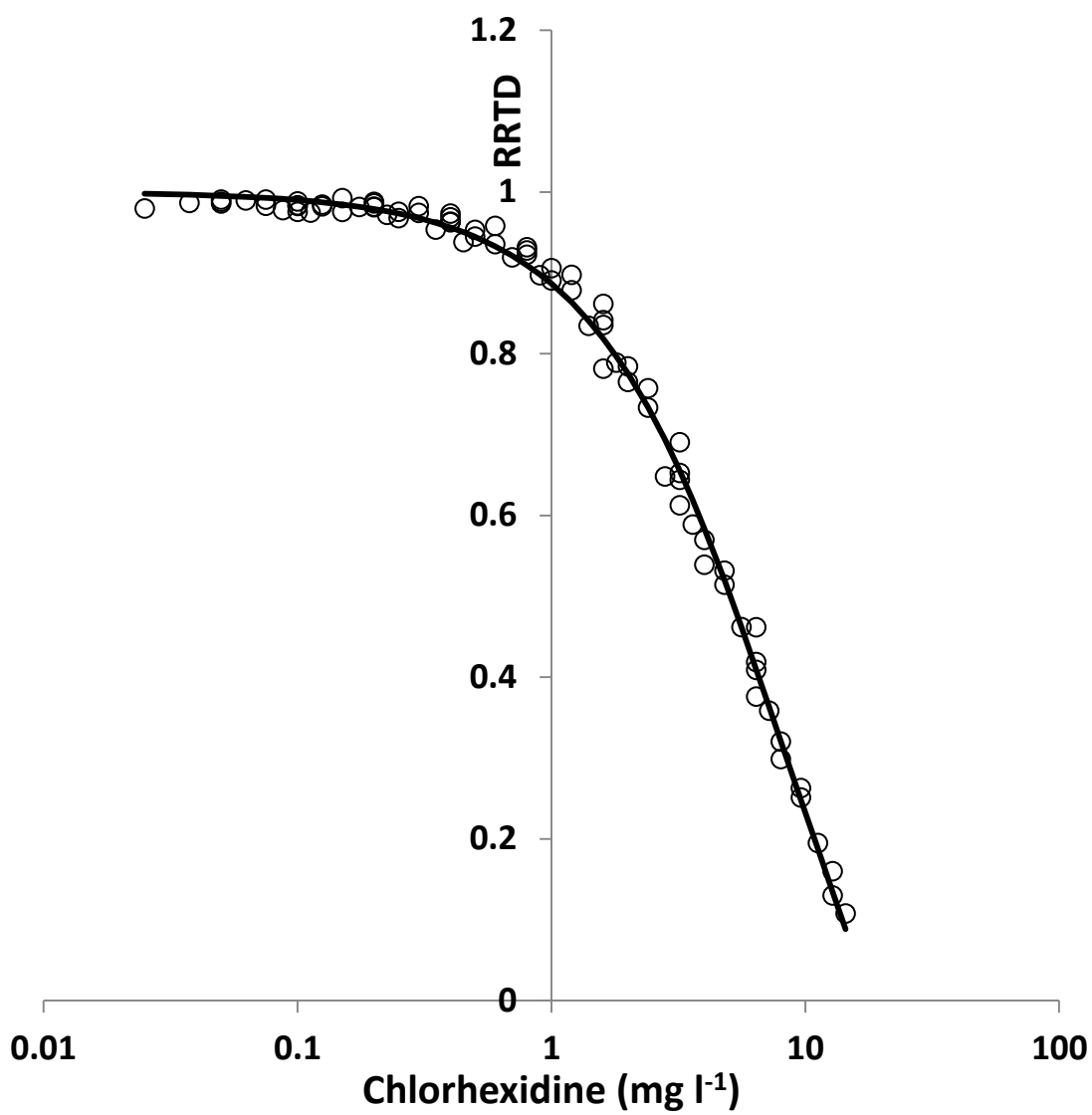
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426 Figure 4

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431 Figure 5

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|     | A       | B         | C                 | D          | E           | F           | CW         | CX         |
|-----|---------|-----------|-------------------|------------|-------------|-------------|------------|------------|
| 1   |         |           |                   |            |             |             |            |            |
| 2   | RMSE    | 0.0218361 |                   |            |             |             |            |            |
| 3   |         | obs       | 1                 | 2          | 3           | 4           | 99         | 100        |
| 4   |         | 1         | -0.0660           | 0.0035     | -0.0189     | 0.0191      | 0.0114     | 0.0003     |
| 5   |         | 2         | -0.0229           | 0.0358     | -0.0234     | 0.0286      | 0.0112     | -0.0121    |
| 6   |         | 3         | -0.0035           | -0.0160    | 0.0043      | 0.0018      | 0.0172     | 0.0013     |
| 82  |         | 79        | -0.0021           | 0.0490     | 0.0411      | 0.0336      | -0.0062    | 0.0169     |
| 83  |         | 80        | 0.0488            | -0.0065    | -0.0240     | 0.0045      | -0.0028    | 0.0234     |
| 84  |         | 81        | -0.0254           | -0.0056    | -0.0149     | -0.0001     | 0.0126     | -0.0125    |
| 85  |         |           |                   |            |             |             |            |            |
| 86  |         |           |                   |            |             |             |            |            |
| 87  | model   | Obs       | 1                 | 2          | 3           | 4           | 99         | 100        |
| 88  | 1       | 1         | 0.93399           | 1.00350    | 0.98109     | 1.01907     | 1.01144    | 1.00026    |
| 89  | 0.99764 | 2         | 0.97477           | 1.03347    | 0.97421     | 1.02628     | 1.00886    | 0.98558    |
| 166 | 0.12804 | 79        | 0.12594           | 0.17699    | 0.16915     | 0.16167     | 0.12181    | 0.14490    |
| 167 | 0.12804 | 80        | 0.17683           | 0.12153    | 0.10406     | 0.13250     | 0.12528    | 0.15140    |
| 168 | 0.07826 | 81        | 0.05288           | 0.07265    | 0.06337     | 0.07815     | 0.09086    | 0.06571    |
| 169 |         |           |                   |            |             |             |            |            |
| 170 |         |           |                   |            |             |             |            |            |
| 171 | Conc    | model     | 1                 | 2          | 3           | 4           | 99         | 100        |
| 172 | 0       | 1         | =IF(\$A172=0,1,IF | 1          | 1           | 1           | 1          | 1          |
| 173 | 0.0375  | 0.99764   | 0.99797           | 0.99771    | 0.99761     | 0.99721     | 0.99773    | 0.99758    |
| 174 | 0.05    | 0.99672   | 0.99716           | 0.99681    | 0.99668     | 0.99616     | 0.99684    | 0.99663    |
| 251 | 12.8    | 0.12804   | 0.12633           | 0.12472    | 0.12574     | 0.13950     | 0.12756    | 0.12732    |
| 252 | 14.4    | 0.07826   | 0.07540           | 0.07465    | 0.07601     | 0.09119     | 0.07749    | 0.07773    |
| 253 |         |           |                   |            |             |             |            |            |
| 254 |         | Mod       | 1                 | 2          | 3           | 4           | 99         | 100        |
| 255 | P1      | 7.1213    | 7.3217            | 7.2238     | 7.2140      | 7.3341      | 7.2728     | 7.2288     |
| 256 | P2      | 1.0796    | 1.1754            | 1.1554     | 1.1478      | 1.1148      | 1.1556     | 1.1444     |
| 257 |         |           |                   |            |             |             |            |            |
| 258 |         | SSE       | 0.044169068       | 0.05177825 | 0.045781245 | 0.040551295 | 0.03294538 | 0.04006947 |
| 259 |         | Tot SSE   | 3.78178           |            |             |             |            |            |
| 260 |         | Target    | 2.18361           |            |             |             |            |            |
| 261 |         |           |                   |            |             |             |            |            |
| 262 | MIC     | 17.9824   | 17.1433           | 17.1647    | 17.2400     | 17.9861     | 17.2793    | 17.3200    |
| 263 | NIC     | 1.4498    | 1.6972            | 1.6327     | 1.6145      | 1.5701      | 1.6441     | 1.6107     |

Figure 6

|                                                                                                                                                                                                                                                                           |          |             |           |                     |         |         |         |    |      |           |                   |         |         |          |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------|-------------|-----------|---------------------|---------|---------|---------|----|------|-----------|-------------------|---------|---------|----------|
| $=(M\$132/(M\$133*\text{SQRT}(\text{PI}()/2)))*\text{EXP}(-2*((\$C5-M\$134)^2/M\$133^2))+((M\$135/(M\$136*\text{SQRT}(\text{PI}()/2)))*\text{EXP}(-2*((\$C5-M\$137)^2/M\$136^2)))+(M\$138/(M\$139*\text{SQRT}(\text{PI}()/2)))*\text{EXP}(-2*((\$C5-M\$140)^2/M\$139^2))$ |          |             |           |                     |         |         |         |    |      |           |                   |         |         |          |
|                                                                                                                                                                                                                                                                           | J        | K           | L         | M                   | N       | DC      | DD      | DE | DF   | DG        | DH                | DI      | GX      | GY       |
| 1                                                                                                                                                                                                                                                                         |          |             |           |                     |         |         |         |    |      |           |                   |         |         |          |
| 2                                                                                                                                                                                                                                                                         |          | MC analysis |           |                     |         |         |         |    |      |           |                   |         |         |          |
| 3                                                                                                                                                                                                                                                                         |          |             |           | Modelled Data       |         |         |         |    |      |           | Virtual data sets |         |         |          |
| 4                                                                                                                                                                                                                                                                         |          | time        | Modelled  | MC1                 | MC2     | MC95    | MC96    |    | time | Modelled  | MC1               | MC2     | MC95    | MC96     |
| 5                                                                                                                                                                                                                                                                         |          | 1.04        | 4.9713675 | 4.96509             | 4.94832 | 4.99872 |         |    | 1.04 | 4.9713675 | 4.8811            | 4.97615 | 4.94275 | 4.98347  |
| 6                                                                                                                                                                                                                                                                         |          | 1.06        | 2.8469856 | 2.83839             | 2.83586 | 2.79671 | 2.81468 |    | 1.06 | 2.8469856 | 2.84638           | 2.80143 | 2.81095 | 2.84357  |
| 126                                                                                                                                                                                                                                                                       |          | 3.46        | 0.0226895 | 0.02001             | 0.02097 | 0.0236  | 0.02328 |    | 3.46 | 0.0226895 | 0.0555            | 0.00527 | 0.06119 | 0.01604  |
| 127                                                                                                                                                                                                                                                                       |          | 3.48        | 0.0186681 | 0.01635             | 0.01718 | 0.01946 | 0.01919 |    | 3.48 | 0.0186681 | 0.02206           | 0.01389 | 0.01855 | -0.03865 |
| 128                                                                                                                                                                                                                                                                       |          | 3.5         | 0.0152933 | 0.0133              | 0.01401 | 0.01598 | 0.01575 |    | 3.5  | 0.0152933 | -0.04361          | 0.00629 | 0.00143 | -0.02886 |
| 129                                                                                                                                                                                                                                                                       |          |             |           |                     |         |         |         |    |      |           |                   |         |         |          |
| 130                                                                                                                                                                                                                                                                       |          |             |           | Parameter Estimates |         |         |         |    |      |           |                   |         |         |          |
| 131                                                                                                                                                                                                                                                                       |          | Parameter   | MOD       | MC1                 | MC2     | MC95    | MC96    |    |      |           |                   |         |         |          |
| 132                                                                                                                                                                                                                                                                       | Pk1      | A1          | 0.6335031 | 0.63389             | 0.62065 | 0.63325 | 0.6421  |    |      |           |                   |         |         |          |
| 133                                                                                                                                                                                                                                                                       |          | w1          | 0.2428981 | 0.24216             | 0.2401  | 0.24353 | 0.24118 |    |      |           |                   |         |         |          |
| 134                                                                                                                                                                                                                                                                       |          | c1          | 1.3963352 | 1.39583             | 1.39741 | 1.39594 | 1.3978  |    |      |           |                   |         |         |          |
| 135                                                                                                                                                                                                                                                                       | Pk3      | A2          | 1.5527126 | 1.5761              | 1.57711 | 1.54235 | 1.536   |    |      |           |                   |         |         |          |
| 136                                                                                                                                                                                                                                                                       |          | w2          | 0.4182147 | 0.42184             | 0.42183 | 0.418   | 0.41376 |    |      |           |                   |         |         |          |
| 137                                                                                                                                                                                                                                                                       |          | c2          | 1.8745919 | 1.87693             | 1.87453 | 1.8731  | 1.8741  |    |      |           |                   |         |         |          |
| 138                                                                                                                                                                                                                                                                       | pK2      | A3          | 1.2868928 | 1.26079             | 1.26732 | 1.30255 | 1.29881 |    |      |           |                   |         |         |          |
| 139                                                                                                                                                                                                                                                                       |          | w3          | 0.6086458 | 0.59643             | 0.60091 | 0.61345 | 0.61288 |    |      |           |                   |         |         |          |
| 140                                                                                                                                                                                                                                                                       |          | c3          | 2.5666363 | 2.57194             | 2.57021 | 2.56324 | 2.56287 |    |      |           |                   |         |         |          |
| 141                                                                                                                                                                                                                                                                       | Artefact | A4          | 5.5773766 | 4.58378             | 5.3543  | 10.6411 | 10.641  |    |      |           |                   |         |         |          |
| 142                                                                                                                                                                                                                                                                       |          | w4          | 0.14447   | 0.14202             | 0.14304 | 0.15886 | 0.158   |    |      |           |                   |         |         |          |
| 143                                                                                                                                                                                                                                                                       |          | c4          | 0.90182   | 0.91032             | 0.90432 | 0.8665  | 0.86763 |    |      |           |                   |         |         |          |
| 144                                                                                                                                                                                                                                                                       |          |             |           |                     |         |         |         |    |      |           |                   |         |         |          |
| 145                                                                                                                                                                                                                                                                       |          | SSE         | 0.09986   | 0.08157             | 0.07409 | 0.09013 | 0.09645 |    |      |           |                   |         |         |          |
| 146                                                                                                                                                                                                                                                                       |          | Tot SSE     | 9.759271  |                     |         |         |         |    |      |           |                   |         |         |          |

Figure 7



**DSPACE**

<https://dspace.org/>

**Monte Carlo simulation of parameter confidence intervals for non-linear regression analysis of biological data using Microsoft Excel.**

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