

The impact of mechanical shear on membrane flux and energy demand

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Abstract

The use of forced mechanical shear for both disc membranes (rotating and vibrating disc filtration, RDF and VDF respectively) and hollow fibres (vibrating HF membranes, VHFM) is reviewed. These systems have been extensively studied and, in the case of the disc membranes, have reached commercialisation and proven effective in achieving transmembrane pressure (TMP) control for various challenging feed waters.

The effects of operating conditions, namely shear rate as enhanced by rotation and vibration speed and TMP, and feed water quality on the filtration flux and specific energy consumption are quantified as part of the review. A new relationship is revealed between the two empirical constants governing the classical relationship between membrane flux and shear rate, and a mathematical correlation proposed accordingly. A study of available information on energy reveals that operation at lower shear rates (i.e. rotation or vibration speeds) and more conservative fluxes leads to lower specific energy demands in kWh m⁻³ permeate, albeit with a larger required membrane area.

Keywords mechanical shear, rotating membranes, vibrating membranes, hollow fibre, specific energy demand

1 Introduction

All membrane processes where there is relative motion between the membrane and the fluid involve shear. In conventional crossflow membrane filtration shear is generated by pumping the liquid through a membrane channel. For a submerged membrane process, and specifically a membrane bioreactor (MBR), it is generated through the action of air bubbles scouring the membrane surface. An alternative to promoting the liquid motion, however, is to apply shear mechanically to move the membrane as opposed to the liquid.

The paper aims to identify possible relationships between flux and membrane motion which determine the nature of the impact of shear on both productivity (i.e. permeate flux) and specific energy demand (energy per unit volume of permeate). These aspects are considered for specifically for both rotating and vibrating membrane technologies of flat disc and hollow fibre membrane configuration.

2 Rotating and vibrating disc filters (RDF and VDF)

2.1 Shear impacts on flux

The use of mechanically-imposed shear to enhance flux by reducing both concentration polarisation (CP) and/or the development of the filter cake is well established [1-3]. Dynamic or shear-enhanced filtration involves creating shear at the membrane by rotating (and thus rotating disc filtration or RDF) or vibrating (hence VDF) the membrane or some component near the membrane surface, with RDFs sometimes using overlapping multiple shaft discs (MSDs). The movement may be either axial or, more usually, torsionally around the axis for disc membranes, or horizontal (lateral) or vertical for rectangular membranes (Fig. 1). Using dynamic filtration has been shown by various investigators [4-11] to greatly suppress CP limitations, reducing the membrane area requirement [12]. The process appears especially effective for high-value, small-scale duties, including various dairy industry applications [6,13-25], the treatment of yeast dispersions and bovine albumin solutions [4,5,26], pulp and paper industry applications [7,27] and specialist beverage process separations, such as the treatment of chicory juice [28,29,30] or sugar beet juice [31,32]. However, it has also found use in landfill leachate treatment [33,34], arsenic removal from drinking water [11,35], treatment of brine and brackish water [36,37,38], removal of natural organic matter [10,39,40], livestock wastewater treatment [8,41,42], dishwasher detergent wastewater and surfactant solution treatment [43-44], separation of microalgae [45, 46] and *Anammox* sludge consolidation [47].

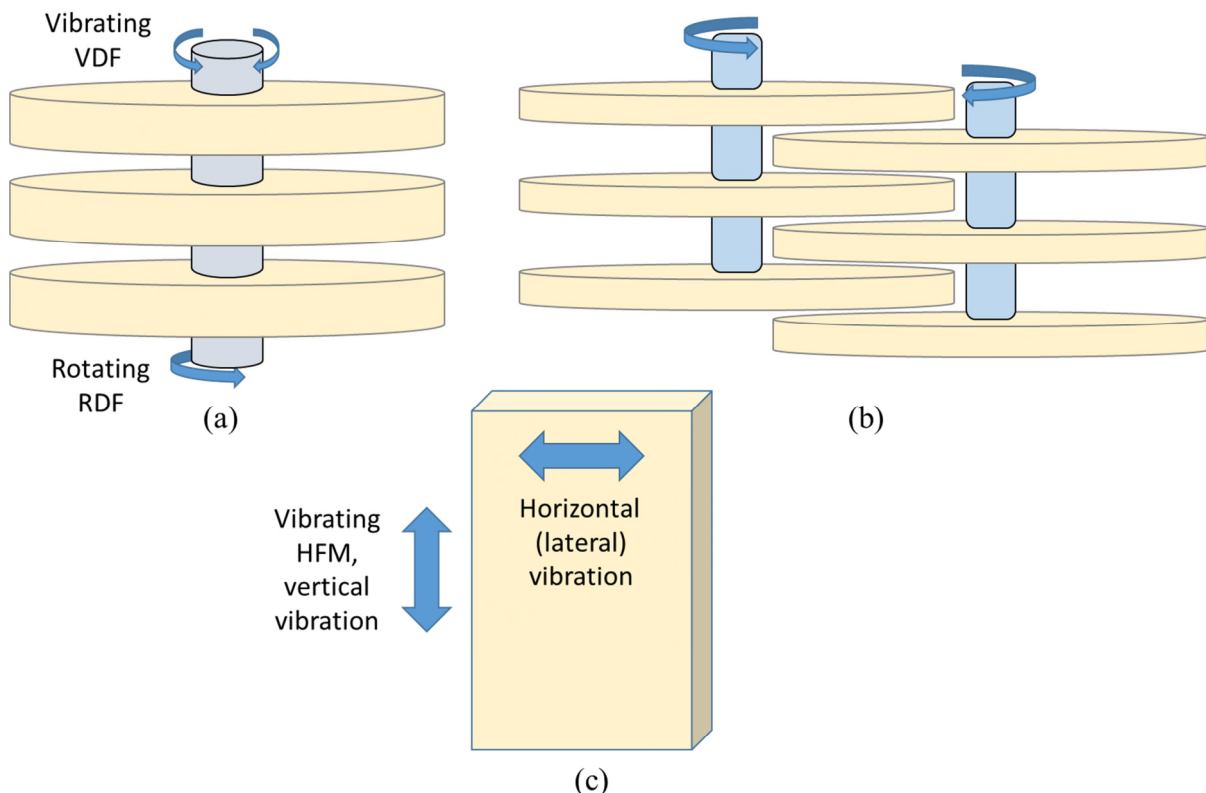


Figure 1. Membrane technologies with modes of movement: (a) rotating and vibrating disc filters (RDF and VDF), indicating torsional motion; (b) multiple shaft disc (MSD), overlapping, (c) vibrating membrane (e.g. hollow fibre, VHF).

Although most dynamic filtration investigations have shown filtration flux to increase with increasing surface shear, the precise relation evidently depends on feed type and concentration [4,5,48], pore size of the applied membrane [5,31,35,40] and system operating conditions [48, 49]. However, the flux generally increases with vibration/rotation rate and amplitude, with rejection capability also affected in some instances [9,36,37,40].

The correlation of flux with shear takes the general form [3]:

$$J = k\gamma^n \quad (1)$$

where γ is the shear rate, in units of inverse time, and k and n are empirical constants. In this simple relationship the coefficient k can be viewed as the strength of the correlation and the exponent n the sensitivity, with respect to flux vs. shear.

A summary of available data for k and n values obtained for primarily vibrating and rotating ultra/microfiltration membrane systems (Table 1) indicates a number of interesting trends:

1. Exponent values relate primarily to feedwater characteristics. For example, reported values of n for skimmed milk, from data derived from four independent studies, lie between 0.48 and 0.60. The value appears independent of either the technology or the membrane characteristics (and specifically the material and pore size),
2. High exponent values are associated with high viscosity, which in turn relates to solid or solute concentration. Examples of such matrices include systems where the feed is being concentrated - sometimes referred to as “volume reduction” [49-51] – or innately high-solids systems such as fermentation broths [51] and soya milk [14-15].
3. There is also some dependence of n on applied pressure [44] across ranges of 0.5-10 bar for RDFs [4,48,49,52], 0.8-15 bar for VDFs [4,48,49,53], up to 3 bar for MSDs [44] and 0.005-0.008 bar for a vibrating hollow fibre membrane (VHFM) [54]. At lower pressures the initial flux has been reported to increase more rapidly with increasing shear than at higher pressures.
4. Exponent values tend to be higher for smaller pore sized (ultrafiltration, UF) membranes, as compared with coarser (microfiltration, MF) ones, under otherwise comparable conditions [5,55].
5. The coefficient value tends to increase with decreasing exponent value, especially at lower shear rate ($<2000 \text{ s}^{-1}$). According to Beier et al. [56], this increase relates to the macromolecular content of the feedwater which tends to lower the critical flux. On the other hand, the exponent trend indicates the rate of flux increase, or the efficacy of the applied shear, and tends to increase with increasing macromolecule content.

Table 1: n and k data for membrane filtration systems

Technol.	Feed	Membrane	Flux (LMH)	Shear rate (s ⁻¹)	Expont.	Coefficient	Source
VDF	UHT skimmed milk	NF - 150-300 Da (Desal)	20-200	11500-107000	1.560	0.00003	[6]
VDF/RDF	Yeast	MF - 0.2 µm (sym. Nylon)	50-550	45000-300000	1.459	0.0000043	[49]
VDF	UHT skim milk	UF - 50 kDa (PES)	20-80	40000-110000	1.257	0.000034	[49]
RDF	Soya milk	UF - 50 kDa (PES)	10-100	23000-200000	0.778	0.0069	[15]
RDF	Soya milk	UF - 50 kDa (PES)	13-100	10000-220000	0.720	0.013	[14]
RDF	Ferm. Biomass, 30° C	MF - 0.2 µm	25-400	5-225 Pa	0.720	4.61	[51]
RDF	Ferm. Biomass, 36° C	MF - 0.2 µm	40-800	6-400 Pa	0.680	17.54	[60]
RDF	UHT skim milk	UF - 50 kDa (PES)	40-300	18000-290000	0.595	0.143	[49]
VDF	UHT skim milk	UF - 50 kDa (PES)	30-100	12000-120000	0.587	0.110	[49]
VDF	UHT skim milk	UF - 50 kDa (PES)	20-70	10000-100000	0.576	0.09	[49]
RDF	UHT skim milk	UF - 50 kDa (PES)	40-170	9000-110000	0.572	0.199	[57]
RDF	UHT skim milk	UF - 50 kDa (PES)	40-105	20000-110000	0.572	0.134	[49]
VDF	UHT skim milk	UF - 50 kDa (PES)	10-60	2800-55000	0.567	0.121	[4]
RDF	Yeast	MF - 0.2 µm (sym. Nylon)	40-80	20000-70000	0.567	0.1402	[49]
VDF	UHT skim milk	UF - 50 kDa (PES)	10-55	2800-70000	0.560	-	[58]
RDF	UHT skim milk	UF - 50 kDa (PES)	50-300	13000-230000	0.552	0.301	[57]
VDF	UHT skim milk	UF - 50 kDa (PES)	15-80	5000-110000	0.533	0.168	[49]
VDF	UHT skim milk	UF - 50 kDa (PES)	15-80	3000-60000	0.533	0.217	[4]
VDF	Powder milk	UF - 10 kDa (PES)	26-55	18000-65000	0.520	0.2	[13]
VDF	Yeast	MF - 0.2 µm (sym. Nylon)	38-65	33000-90000	0.502	0.207	[49]
RDF	UHT skim milk	UF - 50 kDa (PES)	60-200	14000-200000	0.500	0.36	[52]
VDF	Yeast	MF - 0.2 µm (sym. Nylon)	40-70	12000-35000	0.500	0.3489	[48]
RDF	Linseed oil	UF - 50 kDa (PES)	20-180	4000 - 350000	0.477	0.364	[55]
VDF	UHT skim milk	MF - 0.1 µm (PTFE)	20-35	3000-11000	0.476	0.41	[4]
VDF	Powder milk	UF - 10 kDa (PES)	20-90	5000-100000	0.471	0.352	[53]
VDF	Bovine albumin	UF - 50 kDa (PES)	50-120 at 10°C, 90-400 at 35°C	1200-30000 at 10°C, 1700-40000 at 30°C	0.426	2.86 at 10°C, 3.95 at 35°C	[48]
VHFM	Yeast	MF - 0.36-0.5 µm	0-25	0-2000	0.376	2.099	[56]
RDF	Linseed oil	MF - 0.15 µm (PVDF)	30-130	4000-400000	0.364	1.82	[55]
MSD	CaCO ₃	MF - 0.2 µm (ceramic)	300-900	6000-60000	0.351	18.861	[44]
VHFM	Yeast	MF - 0.36-0.5 µm	0-16	0-2000	0.323	1.7887	[56]
MSD	CaCO ₃	MF - 0.2 µm (nylon)	400-800	5000-20000	0.305	38.266	[44]
VHFM	Yeast	MF - 0.36-0.5 µm	15-70	0-2000	0.264	8.2167	[59]
VSEP	UHT skim milk	MF - 0.1 µm (PTFE)	35-50	11000-70000	0.215	4.781	[4]
VSEP	Yeast	MF - 0.2 µm (sym. Nylon)	30-40	2000-12000	0.190	6.619	[48]
VSEP	Yeast	MF - 0.2 µm (sym. Nylon)	28-38	6500-33000	0.189	5.44	[49]
RDF	Yeast	MF - 0.2 µm (sym. Nylon)	30-40	5500-20000	0.186	6.17	[49]

PVDF: Polyvinylidene fluoride; PES: polyethersulphone; PTFE: Polytetrafluoroethylene

Whilst it has been suggested that shear impacts pertain to the technology [49], evidence suggests that there is a universal relationship relating n to k . A correlation of these two parameters reveals a log:normal relationship (Fig. 2), with an R^2 value of 0.98, based on 34 of the 38 data points in Table 1. Thus, for these data, based on units of s^{-1} for shear and LMH for flux in Equation 1:

$$n = (1.98 - \log k)/5.04 \quad (2)$$

Simplifying the two empirical constants in the above equation, Equation 1 becomes:

$$J \sim 10^{(2-5n)} \gamma^n \quad (3)$$

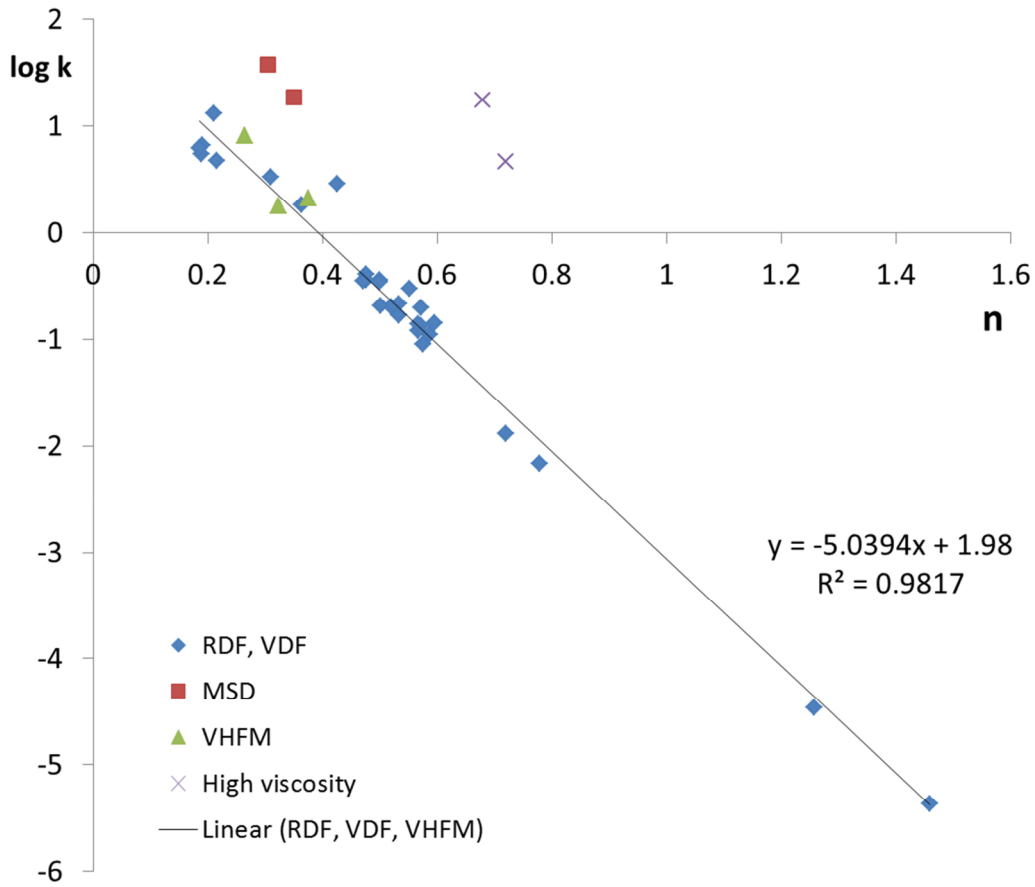


Figure 2. Correlation of n and k parameters in a log:normal relationship

The relationship appears to apply for all data, albeit with a limited data set for the VHFM technology, other than those relating either to the multishaft disk (MSD) technology or to a feedwater matrix comprising extracellular polysaccharides generated by fermentation of biomass at a concentration of 1.4 - 2.5 g/l [51, 60]. For the latter especially, the flux generated is far more sensitive to shear than Equation 3 implies, most likely because of the differing rheological behaviour of this particular fluid [60]. These anomalies aside, for mechanical systems demonstrating classical behaviour the flux sustained by an applied shear can be estimated from Equation 3, provided the exponent value n is known or can be derived.

2.2 Shear impacts on energy demand, disc membranes

Whilst the relationship between the strength (k) and sensitivity (n) parameters shown in Figure 1 is of interest, of greater practical significance is the impact of shear (or rotation speed) on overall energy demand E in kWh per m³ permeate. Such relationships are specific to the disc membrane technology and size, since the total energy required to rotate shaft is only marginally affected by the number of discs attached to it. The absolute energy demand thus decreases significantly, from several hundred kWh per m³ permeate for a single disc [61] with the increasing number of discs on the shaft. Trends in energy demand, on the other hand, may not necessarily be dependent on the number of discs.

The energy consumption per m³ permeate (specific energy demand, E) for a single RDF is represented by

$$E = W_d / Q_f \quad (4)$$

where W_d is the sum of power of the rotating disk motor and feed pump (kW) and Q_f is the permeate flow rate (m³.h⁻¹) and has been defined as [21]:

$$W_d = 0.141 \exp(0.000756 N) \quad (5)$$

where N is the rotating speed of disk motor (RPM).

However, power has also been defined solely in terms of the friction forces exerted by the fluid [51]. The net power W_N is then given by the difference between the power demanded with the fluid in place (W_d) and that without the fluid (W_o) determined at the same speed:

$$W_N = W_d - W_o \quad (6)$$

This definition leads to significantly lower values of E with a more pronounced dependency on shear (or rotation speed) due to the rapid decrease in friction forces at low shear.

Notwithstanding the nature of its definition, correlations of the change in E with key system parameters (Table 2) based on data reported by various authors [21,28,30,51,52,55,60] for single-disc studies indicate significant differences in such correlations across the different studies. Thus, an increased membrane pore size has been shown to both increase [28] and decrease [21] the energy demand by factors of between 1.5 and 2.2 depending on the membrane and suspended matter characteristics, feed concentration, and operating pressure. However, there appears to be a threshold value beyond which further shear does not increase the flux [44], such that E always increases beyond this point. The solute or suspended matter concentration, as implied by the volume reduction rate (VRR) has been shown to increase the absolute value of E but not the trend against shear rate [21].

More representative absolute E values are provided by systems based on multiple discs on either single or multiple shafts. Figures reported for demonstration and commercial RDF systems (Table 3) indicate E values predominantly in the range of 0.7-11 kWh m⁻³ [16,44,45,57] based on the definition of E (Equation 6) provided by Brou et al., [51], and 3-6 kWh m⁻³ based on the classical definition (Equation 4). In the case of commercial VDF systems, the most prominent being the established *V-Sep* technology, E values within a relatively narrow range have been reported; 1.8 kWh.m⁻³ for skimmed milk and brackish water [53] cf. to 2.1 kWh.m⁻³ for brackish water desalination [38]. A recently commercialized RDF system for biological wastewater treatment applications [63] operates at the lowest rotation speeds on 100-140 RPM and provides the lowest E value (0.63 kWh.m⁻³) of those tabulated.

Table 2: Published RDF data, bench-scale

<i>Membrane, RDF technology</i>	<i>Matrix</i>	<i>Parameter change, γ, N, d_p, P, C^2</i>	<i>P (bar)</i>	<i>Flux range (LMH)</i>	<i>E factorial change</i>	<i>E Equation</i>	<i>Ref</i>
50 kDa, 6mm	Chicory Juice	γ , 8.5-fold increase from 12,000 s ⁻¹	2	172-426	2.48	5	[44]
50 kDa, 6mm	Chicory Juice	γ , 8.5-fold increase from 12,000 s ⁻¹	4	155-431	2.78	5	[44]
50 kDa, 6mm	Chicory Juice	γ , 8.5-fold increase from 12,000 s ⁻¹	4	251-716	2.85	5	[44]
0.15, 0.2, 0.45 μ m, 100 kDa, 6mm vanes	Chicory Juice	d_p , 0.15-0.45 μ m, N , 1000-2000 RPM; γ , 3.4-fold increase from 73,000 s ⁻¹	0.75	60-320	1.7-2.5	5	[28]
MF, smooth	Fermentation biomass	N , 5-fold increase from 500 RPM; P , 20-25-fold increase from 6 Pa	<0.3	25 - 200	9.2	6	[51]
MF, 6mm vanes	Fermentation biomass	N , 5-fold increase from 500 RPM; P , 20-25-fold increase from 6 Pa	<0.6	40- 400	11.3	6	[51]
MF, 2mm vanes	Fermentation biomass	N , 5-fold increase from 500 RPM; P , 20-25-fold increase from 6 Pa	<0.6	35 - 370	10.0	6	[51]
MF, smooth	Baker's yeast	N , 5-fold increase from 500 RPM	<0.9	60 -300	8.7	6	[60]
MF, 6mm vanes	Baker's yeast	N , 5-fold increase from 500 RPM	<1.2	150 - 600	11.5	6	[60]
MF, 6mm vanes	Baker's yeast	N , 5-fold increase from 500 RPM	<1.2	300 - 1000	30	6	[60]
PVDF, 0.15 μ m, with vanes	Linseed oil	N , 5.5-fold increase from 500 RPM; γ , 22-24-fold increase from 12,000 s ⁻¹	<0.9	35 - 130	7.8	6	[55]
PVDF, 0.15 μ m, smooth disk	Linseed oil	N , 5.5-fold increase from 500 RPM; γ , 22-24-fold increase from 12,000 s ⁻¹	<0.35	18 - 95	6	6	[55]
PES 50 kDa disk with vanes	Linseed oil	N , 5.5-fold increase from 500 RPM, γ , 22-24-fold increase from 12,000 s ⁻¹	<0.4	20 - 170	8.8	6	[55]
PES 50 kDa smooth disk	Linseed oil	N , 5.5-fold increase from 500 RPM; γ , 22-24-fold increase from 12,000 s ⁻¹	<1	12 - 95	7	6	[55]
NF270 ¹ , 6 mm vanes	Skimmed milk	C , ~4-fold increase (through volume reduction rate, VRR)	10	100-500, 100-210	2.08	5	[64]
NF270 ¹ , 6 mm vanes	Skimmed milk	P , 2-fold increase from 20 bar, VRR, 4-fold increase	-	1000-350, 45-100	0.3-0.5	5	[64]
PES 50 kDa smooth and small disk	UHT skim milk	N , 5-fold increase from 500 RPM	2 @ 45°C	50 - 130	11.3	6	[57]
PES 50 kDa small disk with vanes	UHT skim milk	N , 5-fold increase from 500 RPM	2 @ 45°C	40 - 145	30	6	[57]

PVDF: Polyvinylidene fluoride; PES: polyethersulphone; ¹proprietary membrane; ²solute concentration;

Table 3: Published RDF and MSD data, demonstration/commercial scale: response of SED to specific parameters

<i>Commercial technology</i>	<i>Matrix</i>	<i>Parameter change</i>	<i>Conditions</i>	<i>SED, kWh.m⁻³</i>	<i>Ref</i>
<u><i>Rotating</i></u>					
<i>Aaflowsystem</i> , 6 discs/shaft	Mineral suspension, 200 g/L	<i>N</i> = 738 to 1930 RPM	SS., P = 2.3 bar, J= 500-1421 LMH	8.04 to 4.18	[61]
<i>Aaflowsystem</i> , 6 discs/shaft	Mineral suspension, >200 g/L	<i>N</i> = 738 to 1930 RPM	DS., P = 2.3 bar, J= 525-1207 LMH	8.67 to 6.9	[61]
<i>Aaflowsystem</i> , 6 discs/shaft ¹	Mineral suspension, >200 g/L	<i>N</i> = 738 to 1037 RPM	DS., P = 3.5 bar, J=1000-1200 LMH, vanes	7 to 5.6	[62]
<i>Westfalia</i> , 6 discs/shaft ² , DS.	Mineral suspension, 200 g/L	<i>N</i> = 400 to 1900 RPM	Cer. memb., P = 3 bar, J=600-1300 LMH	0.75 to 6.5	[44]
		<i>N</i> = 400 to 1900 RPM	Polym memb., P = 3 bar, J=600-1700 LMH	1.75 to 11	[44]
<i>Westfalia</i> , 6 discs/shaft ² , DS.	Skimmed milk	<i>N</i> = 1500 RPM	Cer. memb., P = 6 bar, J= 86.7	10.8	[16]
<i>Spintek</i> , 25-disc unit (2.25 m ²)	River water screen solids	<i>C</i> = 0.6-5 wt%	Cer. memb., P = 2.7-4 bar	22 to 33	[65]
		<i>C</i> = 0.06-1.29 wt%	Cer. memb., P = 2.7-4 bar, J=10.6-4.1 LMH	9.12 to 23.63	[65]
<i>Novoflow</i> , 75-disk unit (15 m ²)	Multiple purpose		SS, 0-6 bar, J = 33-67 LMH	6 to 3	[39, 67,68]
<i>Biobooster</i> , 36 disc unit	MBR sludge	<i>N</i> = 100-140 RPM	Cer. memb., 35 LMH, 0.44 bar	0.63	[63]
<u><i>Vibrating</i></u>					
<i>V-Sep</i> , 0.5 m ² unit	Skimmed mik	<i>N</i> = 60.75 Hz	Polym. memb., P= 8 bar, J=75 LMH,	1.83	[53]
<i>V-Sep</i> ,	Brackish water	<i>N</i> = 60.75 Hz	Recovery= 75%, J=20.4 LMH	2.1	[38]

SS Single shaft; DS dual shaft (overlapping); Cer. ceramic; Polym. polymeric

¹6 ceramic membranes on one shaft with 6 non-permeating metallic membranes on the other. 750 rpm metallic disc²6 ceramic or 6 polymeric disks on one shaft and 3 metal disks on the other

It can be generally surmised from the data in Tables 2 and 3 that an increase in shear generally provides higher fluxes and thus reduces the membrane area requirement, with an expected commensurate decrease in capital cost. However, it does not necessarily follow that there is an accompanying decrease in E – even for full-scale commercial systems. The data in Table 3 suggest that the optimum rotation/vibration rate is likely to be at lower speeds.

3 Vibrating hollow fibre membranes (VHFM) and rotating flat sheet membranes (RFSMs)

The application of mechanical shear to a conventional hollow fibre (HF) and flat sheet (FS) membrane module is a relatively recent area of research, normally relating to immersed membrane bioreactors (iMBRs) but with experimental studies predominantly based on analogues (Table 4). The latter have included macromolecules such as baker's yeast solution [26,54,56,59,69] and bentonite [70,71] or particulate such as alginate [70] to mimic foulants or kaolin suspensions [64], with three reported studies of MBR sludge [72-75]. Data from the single VHFM study in which shear rates are reported [56, 59] are included in Table 1 and Figure 1. Shears attainable for such systems, which have employed a wide variety of motion types, are at the low end ($20\text{-}2000\text{ s}^{-1}$) of those attainable for disc membrane technologies - where the maximum shear is only limited by the rotation speed. However, as is evident from Fig. 1, the quantitative impact of shear on flux for HF and FS membranes does not differ from that recorded for disc membranes; Equation 3 appears to be applicable for enforced-shear systems generally.

Quantitative improvements in flux values, reaching values as high as 70 LMH, have been recorded from the application of shears of up to 2000 s^{-1} to VHFM systems [59] for vertical vibration. Even higher fluxes of 130 LMH were reached on applying both transverse and vertical movement [59]. For other studies at lower applied shears ($1200\text{-}1400\text{ s}^{-1}$), fluxes achieved were commensurately lower (30-60 LMH). Frequencies and amplitudes applied have varied from 6 to 30 Hz and 2 to 40 mm respectively, with some equivocation as to which of these parameters is of greatest importance in promoting flux [59,64].

As with RDS and VDS technologies, E values for VHFM studies are not often reported and are most valid for larger systems. However, the general trend is for comparatively low vibration rates, with values as low as 1.7 Hz [69] and 0.38 Hz [72,73,76] being reported. This leads to commensurately low shear rates, but also low power consumption. Consequently, relatively modest fluxes (in the region of 30-40 LMH) can yield average E values of around 0.91 kWh.m^{-3} , as demonstrated for a vertical VHFM MBR system [72,73,76]. Specific energy demand was lowered from 0.29 to 0.15 kWh m^{-3} and fluxes increased from 46 to 86 LMH when combined vertical and horizontal displacement was applied using turbulence promoting attachments (vanes) along with aluminum chlorohydrate (ACH) coagulant for a VHFM MBR system [69]. An RFSM system operating at low rotation speeds (5 RPM), with a commensurately low power, has been reported as attaining a flux of 105 LMH when challenged with a skimmed milk feed, yielding an E of 0.53 kWh.m^{-3} [26].

The VHFM studies appear to be similar in principle to the RDS Grundfos *Biobooster* technology (Table 2, [63]), which operates at a frequency of 1.6 to 2.3 Hz with a correspondingly conservative flux (35 LMH). However, the reported E of 0.63 kWh/m^{-3} for membrane permeation is significantly higher than the corresponding value for the VHFM challenged with a similar matrix of 8-14 g/L activated sludge [72,73,76].

Table 4: Reported data, VHFM and RFSM technologies

Displacement	Feed solution/application	Membrane material, pore size, area	Maximum flux (LMH)	Vibrating/rotating frequencies (Hz, r/min) amplitude (A)	Shear rate (1/s)	SED (kWh/m ³)	Source
Horizontal (FS)	Aerobic sludge, 10-12 g/l	PE, 0.22 µm, 0.096 m ²	16	0-60 Hz, 0-2 mm	-	2.03	[78]
Horizontal (FS)	Microalgal broths, -	PVDF, 0.036 and 0.013 µm, 4 m ²	>50	45 Hz	-	0.77-0.84	[79]
Rotational	Anaerobic sludge, 8-10 g/L	PVDF, 0.04 µm, - 0.047 m ²	10	4.3 Hz	-	-	[75]
Horizontal	Aerobic sludge, 8-10 g/L	PVDF, 0.04 µm, -	40	0.38-0.48 Hz	-	0.072 (40 LMH, 18 kPa)	[72, 73,76]
Axial (vertical) and lateral movement	Bentonite clay	PAN, 0.1 µm, -	30	10 Hz, 5 mm	-	16.6 W (10 Hz, 5 mm)	[71]
Transverse ¹ membrane movement (A); liquid oscillation (B)	Baker's yeast (4 g/l)	PVDF, 0.04 µm, -	A:40, B:35 (250% enhancement)	A and B: 21.8 Hz, 2.5 mm	-	0.20 (30 LMH, 21.8 Hz, 2.5 mm displacement)	[72]
Vertical vibration	Baker's yeast	PP, 0.2 µm, -	60	1.67–8.35 Hz, 40 mm	0-1402	-	[56]
Vertical vibration	Pottery clay with high kaolin content	PAN, 0.1-0.2 µm, 3.15 m ²	34	6-8 Hz, 8 mm	-	-	[64]
Vertical vibration	Separation of protein (BSA) from baker's yeast suspension	PES/PVP (98/2%), 0.3-0.5 µm, 0.0084 and 0.0488 m ²	30	20 Hz, 1.375 mm	0-1230	-	[80]
Vertical vibration	Separation of enzyme from baker's yeast suspension	PES, 0.36-0.5 µm, 0.0488 m ²	16, 25	5-25 Hz, 0-0.7 mm	0-1200	-	[56]
Vertical vibration	Baker's yeast suspension (5 g/l)	PES, 0.36-0.5 µm	A: 70 (325% enhancement)	5-30 Hz, 0-1.175 mm	22-1936	-	[59]
Vertical (A), and both vertical and transverse ¹ movement (B)	Poly-dispersed yeast cells	0.2 µm, 0.0057 m ²	A: 46, B: 86	0-10, 2 mm	0-2000	0.29 (A:1.7 Hz, 34 ppm ACH); 0.15 (B: 1.7 Hz, vanes ² , 34 mg/L ACH)	[69]
Rotational (Rotating FS)	Baker's yeast suspension (4.9 g/l)	PP-NWF, 3 µm, 0.09 m ²	105	5 rotations/min	-	0.53	[26]
Rotational (Round FS)	Synthetic sewage, MLSS 7-10 g/l	PVDF, 0.2 µm, 0.12 m ²	42.5-47.5	15-25 rotations/min	-	-	[81]

PVDF: Polyvinylidene fluoride; PP: Polypropylene; PAN: Polyacrylonitrile; PES: polyethersulphone; PVP: polyvinylpyrrolidone; PP-NWF: polypropylene nonwoven fabric

¹Transverse: crossflow, tangential ; ²vanes: Vanes were inserted horizontally across the cartridge in a “chess” pattern to promote shear at the membrane surface [69]

The only comparable commercial process in terms of energy demand is the established Huber *Vacuum Rotating Membrane* (VRM) technology. This process employs a membrane which rotates at a speed of only ~ 2 rpm. For this very low rotation speed, the specific energy demanded for the mechanical component of the operation is in the region of 0.015 kWh/m^3 permeate [77] – around 40 times less than that for an RDF technology such as the *Biobooster*. However, the Huber system demands supplementary air scour, adding significantly to the total energy demand. For systems such as the *Biobooster* and the VRM, intended for bulk wastewater treatment at flows of $500\text{--}5000 \text{ m}^3/\text{d}$, the total specific energy demand is of pivotal importance. Against, for “high-end” separations where volumes treated are much smaller, there is less onus on reducing energy and more on control of the process mass transfer that the applied shear permits.

4 Conclusions

Outputs from a review of available data from studies of rotating and vibrating membrane filters (RMF and VMF), as well as those for a vibrating hollow fibre membrane (VHFM), suggest that there is an overall unifying relationship between flux and shear. With the exception of a few anomalous data relating to either multi-shaft systems or unusually high-viscosity (or possibly more generally rheologically distinguished) liquid matrices, most available data suggest that the flux, in LMH, is given approximately by $10^{(2-5n)}\gamma^n$ for shear γ expressed in units of s^{-1} . The strength and sensitivity parameters (the coefficient and exponent respectively) thus appear to be related.

Evidence provided by available information on energy demand for commercial-scale equipment suggests that mechanically-imposed shear in membrane processes becomes more energy efficient in terms of kWh.m^{-3} permeate at lower shear rates (i.e. rotation or vibration speeds) and commensurately more conservative fluxes. Specific energy demands as low as 0.1 kWh m^{-3} have been demonstrated for VHFMs operating at vibration rates below 0.5 Hz (or 30 RPM equivalent) for biological municipal wastewater treatment. This compares with the values of $100\text{--}400 \text{ RPM}$ or 60.75 Hz typically respectively employed for RDF and VDF commercial systems dedicated to high-end, low-volume applications. These appear to operate in the range of $0.6\text{--}2 \text{ kWh.m}^{-3}$, somewhat higher than the VHFM systems but also offer higher fluxes and thus a reduced membrane area requirement. There is thus the classic trade-off between CAPEX and OPEX based on both the technology and the application for these technologies.

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